

# ENT125

## BUSINESS STATISTICS



Course video is available on our app

# Series 1: Foundations and Role of Business Statistics

## Series outline

- **Part 1.1 Nature and Scope of Statistics**
  - 1.1.1 Definition and meaning of statistics
  - 1.1.2 Branches of statistics: descriptive and inferential
  - 1.1.3 Importance of statistics in business decision-making
- **Part 1.2 Statistical Inquiries: Forms and Design**
  - 1.2.1 Types of statistical inquiries
  - 1.2.2 Designing effective statistical investigations
  - 1.2.3 Limitations of statistical inquiries
- **Part 1.3 Role of Statistics in Business and Economics**
  - 1.3.1 Applications of statistics in business performance measurement
  - 1.3.2 Use of statistics in market surveys and research
  - 1.3.3 Ethical considerations in statistical practice
- **Part 1.4 Basic Concepts in Statistics**
  - 1.4.1 Variables: discrete and continuous
  - 1.4.2 Functional relationships in statistics
  - 1.4.3 Sources of statistical data

## Introduction

In today's business environment, decisions are rarely made on intuition alone. Organisations rely on facts, figures, and patterns to guide their strategies, and this is where statistics becomes indispensable. By learning the foundations and role of business statistics, you will be equipped to see how numbers tell stories, how data supports decisions, and how statistical thinking underpins effective management and research. This Series sets the stage for the rest of the course by introducing you to the essential concepts and applications of statistics in business.

The aim of this Series is to familiarise you with the nature, scope, and role of statistics, and to provide you with the basic tools needed to appreciate its importance in business and economics. It intends to build a strong foundation that will support your progress through the more technical aspects of the course.

We shall commence this Series by examining the nature and scope of statistics, including its definition, branches, and importance in business decision-making. Next, we will explore statistical inquiries, focusing on their forms, design, and limitations. Following that, we will move on to the role of statistics in business and economics, considering its applications in performance measurement, market surveys, and ethical practice. Finally, we will wrap up by discussing basic concepts in statistics such as variables, functional relationships, and sources of data. This sequential flow will ensure that you gain a clear and structured understanding of the foundations of business statistics.



# Series Learning Outcomes

Upon completing this Series, you should be able to:

- 2.1 define statistics and distinguish between its descriptive and inferential branches,
- 2.2 explain the importance of statistics in business decision-making,
- 2.3 identify and describe different forms of statistical inquiries,
- 2.4 analyse the key elements involved in designing statistical investigations,
- 2.5 evaluate the role of statistics in measuring business performance and conducting market surveys,
- 2.6 discuss ethical considerations in the application of statistics,
- 2.7 differentiate between discrete and continuous variables,
- 2.8 explain functional relationships in statistics, and
- 2.9 classify sources of statistical data relevant to business research.

## 1.1 Nature and Scope of Statistics

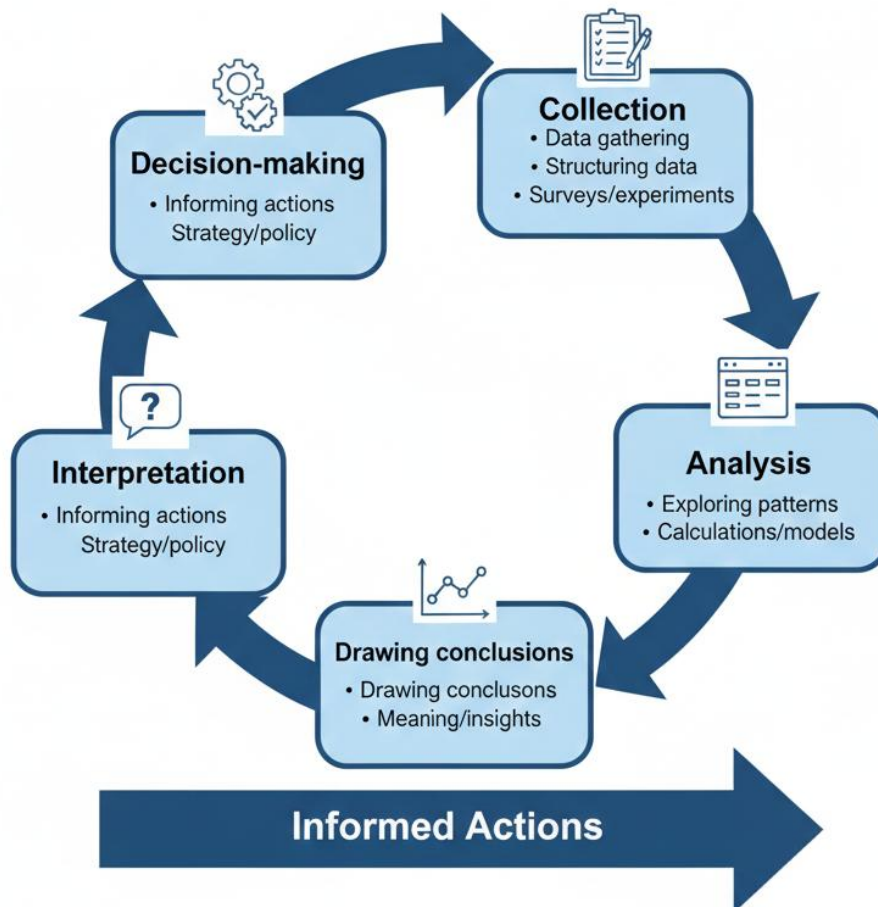
### 1.1.1 Definition and meaning of statistics

**Statistics** refers to the science of collecting, organising, analysing, and interpreting data in order to make informed decisions. In business, statistics provides a systematic way of understanding patterns and trends, rather than relying on guesswork. It is both a body of methods and a field of study that helps managers and researchers to deal with uncertainty.

Fill in the blank: Statistics is the science of \_\_\_\_\_, organising, analysing, and interpreting data.



## Figure 1.1 Statistical process cycle



OER diagram

### 1.1.2 Branches of statistics: descriptive and inferential

**Descriptive statistics** involves summarising and presenting data in a meaningful way, often using measures such as averages, percentages, charts, and graphs. It answers the question: “What does the data show?” **Inferential statistics** goes further by using sample data to make generalisations or predictions about a larger population. It answers the question: “What can we conclude beyond the data we have?”

Fill in the blank: \_\_\_\_\_ statistics summarises data, while inferential statistics makes predictions about populations.



## Table 1.1 Comparison of Descriptive and Inferential Statistics

| Characteristic    | Descriptive Statistics             | Inferential Statistics                             |
|-------------------|------------------------------------|----------------------------------------------------|
| <b>Definition</b> | Summarizes data features           | Draws conclusions about a population from a sample |
| <b>Purpose</b>    | Describe sample/population         | Make predictions/generalizations                   |
| <b>Example</b>    | Average age of students in a class | Predicting election results from a survey          |

OER table

### 1.1.3 Importance of statistics in business decision-making

Statistics is vital in business because it provides evidence-based insights. Managers use statistical tools to evaluate performance, forecast demand, measure customer satisfaction, and assess risks. For example, a company may analyse sales data to determine which products are performing well and which need improvement.

Fill in the blank: Managers use statistics to evaluate \_\_\_\_\_, forecast demand, and assess risks.





Plate 1.1 Business team using statistics for decision-making

OER image

#### Pilot questions 1.1

1. Which branch of statistics focuses on summarising data?
2. Which branch of statistics makes predictions about populations?
3. What is the primary aim of statistics in business decision-making?
4. Fill in the blank: Statistics is the science of collecting, \_\_\_\_\_, analysing, and interpreting data.
5. Give one example of how a business might use statistics to improve performance.

#### 1.2 Statistical Inquiries: Forms and Design

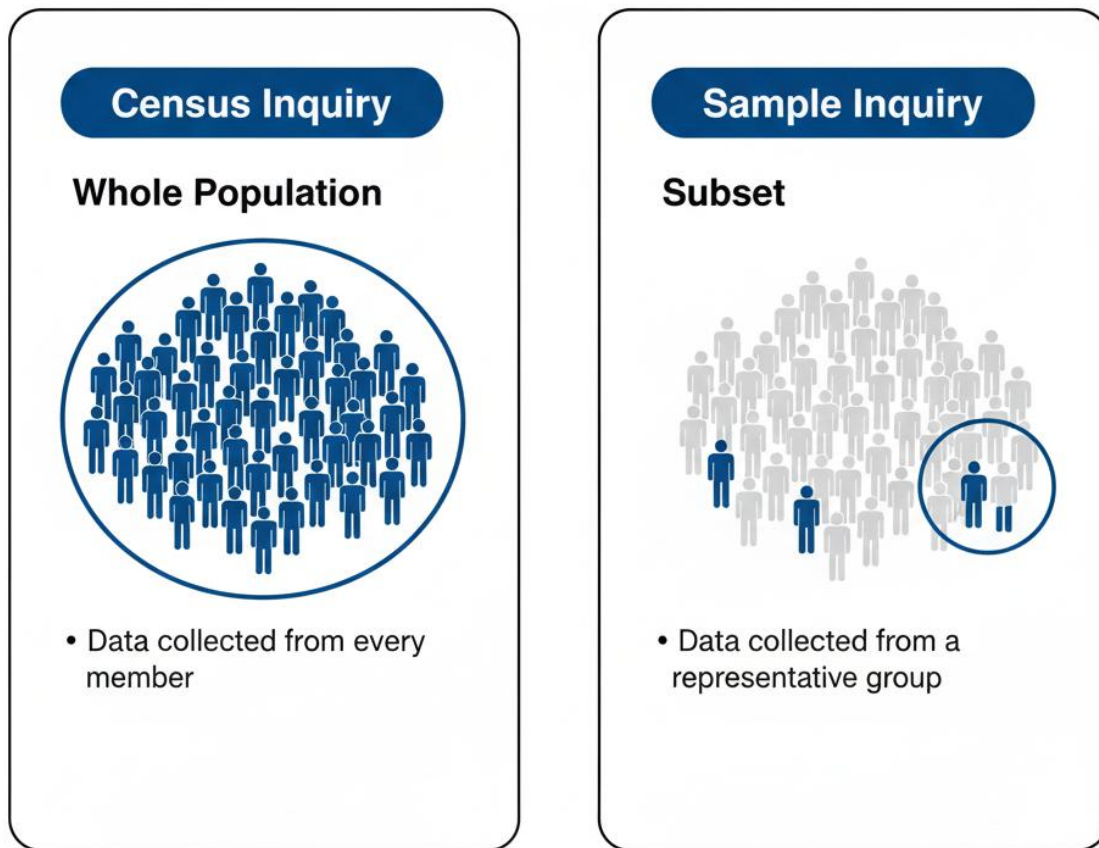


### 1.2.1 Types of statistical inquiries

A **statistical inquiry** is a structured investigation that uses data to answer specific questions or solve problems. In business, statistical inquiries may focus on areas such as customer behaviour, employee performance, or market trends. These inquiries can be classified into different types, including census inquiries, where data is collected from the entire population, and sample inquiries, where data is collected from a subset of the population.

Fill in the blank: A census inquiry collects data from the \_\_\_\_\_ population, while a sample inquiry collects data from a subset.

## Figure 1.2 Types of Statistical Inquiries



OER diagram

### 1.2.2 Designing effective statistical investigations



The design of a statistical investigation is crucial because it determines the reliability of the results. A well-designed inquiry begins with a clear definition of the problem, followed by the identification of objectives, selection of appropriate methods, and determination of the population or sample. It also involves choosing suitable tools for data collection and ensuring that the process is unbiased.

Fill in the blank: A well-designed statistical investigation begins with a clear definition of the \_\_\_\_\_.

### **Box 1.1 Key steps in designing a statistical investigation**

- Defining the problem
- Setting objectives
- Selecting methods
- Ensuring unbiased data collection

OER summary

#### 1.2.3 Limitations of statistical inquiries



Although statistics is powerful, it has limitations. Results may be affected by errors in data collection, biased sampling, or misinterpretation of findings. For instance, if a survey is conducted only among urban customers, the results may not represent rural customers. Moreover, statistics cannot always capture qualitative aspects such as emotions or motivations.

Fill in the blank: Statistics may fail to capture qualitative aspects such as \_\_\_\_\_ or motivations.



Plate 1.2 Limitations in statistical inquiries OER image

#### Pilot questions 1.2

1. What is the difference between a census inquiry and a sample inquiry?
2. What is the first step in designing a statistical investigation?
3. Why is unbiased data collection important in statistical inquiries?



4. Fill in the blank: Statistics may fail to capture qualitative aspects such as \_\_\_\_\_.
5. Give one example of a limitation of statistical inquiries in business research.

### 1.3 Role of Statistics in Business and Economics

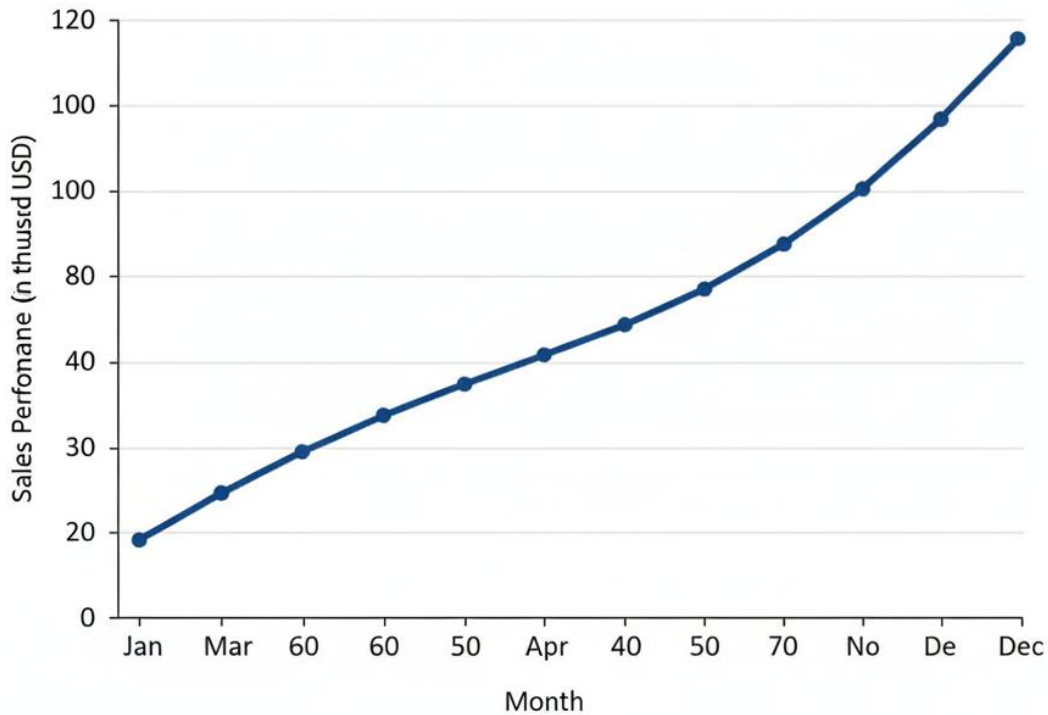
#### 1.3.1 Applications of statistics in business performance measurement

**Business performance measurement** refers to the process of assessing how well an organisation is achieving its objectives. Statistics provides tools such as ratios, averages, and trend analysis to evaluate sales, productivity, and profitability. For example, a company may use statistical charts to compare monthly sales figures and identify growth patterns.

Fill in the blank: Statistics provides tools such as ratios, averages, and \_\_\_\_\_ analysis to evaluate performance.



Figure 1.3 Statistical tools for business performance measurement



OER diagram

### 1.3.2 Use of statistics in market surveys and research

**Market surveys** are investigations conducted to gather information about consumer preferences, buying habits, and product demand. Statistics plays a central role in designing surveys, analysing responses, and drawing conclusions. For instance, a company may use sampling techniques to survey a group of customers and then apply statistical methods to generalise the findings to the wider market.

Fill in the blank: Market surveys are investigations conducted to gather information about consumer \_\_\_\_\_ and product demand.





### Plate 1.3

Conducting market surveys using statistics OER image



#### 1.3.3 Ethical considerations in statistical practice

**Ethical considerations** in statistics involve ensuring honesty, fairness, and transparency in the collection, analysis, and reporting of data. Misrepresentation of data, biased sampling, or selective reporting can lead to misleading conclusions and poor business decisions. Ethical practice requires that statisticians present findings accurately and respect the confidentiality of respondents.

Fill in the blank: Ethical practice requires statisticians to present findings accurately and respect the \_\_\_\_\_ of respondents.



### **Box 1.2 Ethical principles in statistical practice**

- Honesty
- Transparency
- Confidentiality

OER summary

#### **Pilot questions 1.3**

1. Which statistical tools can be used to measure business performance?
2. What is the main purpose of market surveys in business research?
3. Fill in the blank: Market surveys gather information about consumer \_\_\_\_\_ and product demand.
4. Why are ethical considerations important in statistical practice?
5. Give one example of unethical statistical practice that could mislead business decisions.

#### **1.4 Basic Concepts in Statistics**

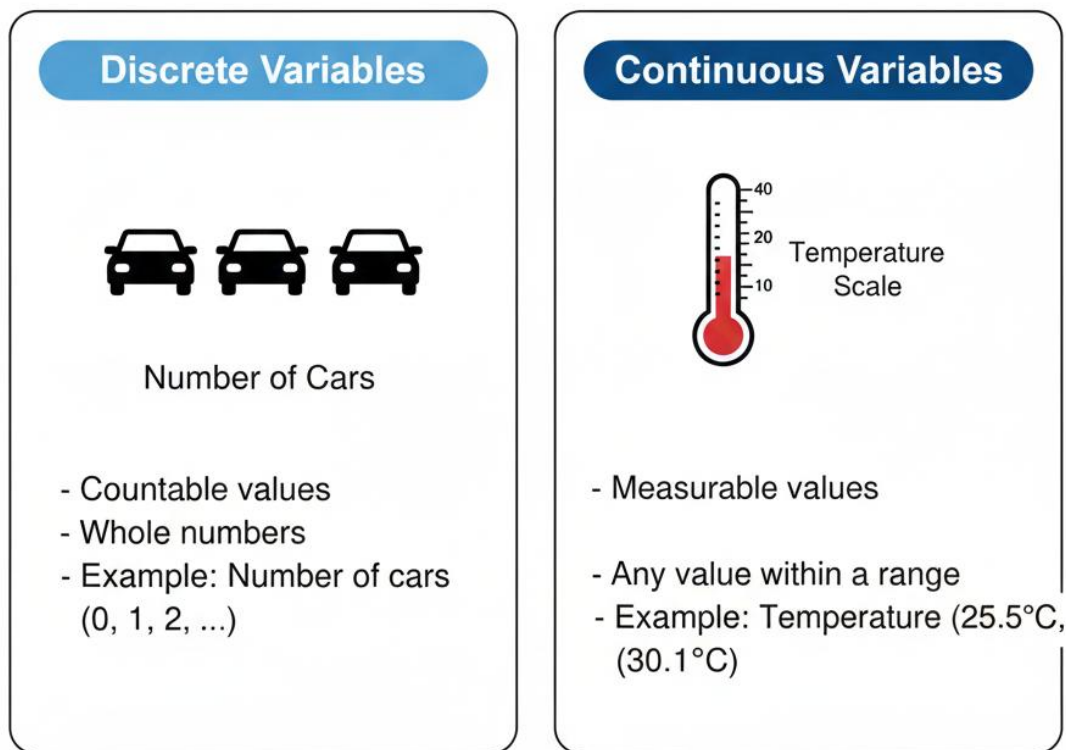


#### 1.4.1 Variables: discrete and continuous

A **variable** is any characteristic or attribute that can take different values. In statistics, variables are classified into two main types. **Discrete variables** are those that take distinct, separate values, often whole numbers, such as the number of employees in a company. **Continuous variables** can take any value within a given range, such as the height of individuals or the daily temperature.

Fill in the blank: The number of employees in a company is a \_\_\_\_\_ variable, while height is a continuous variable.

**Figure 1.4 Discrete and Continuous Variables**



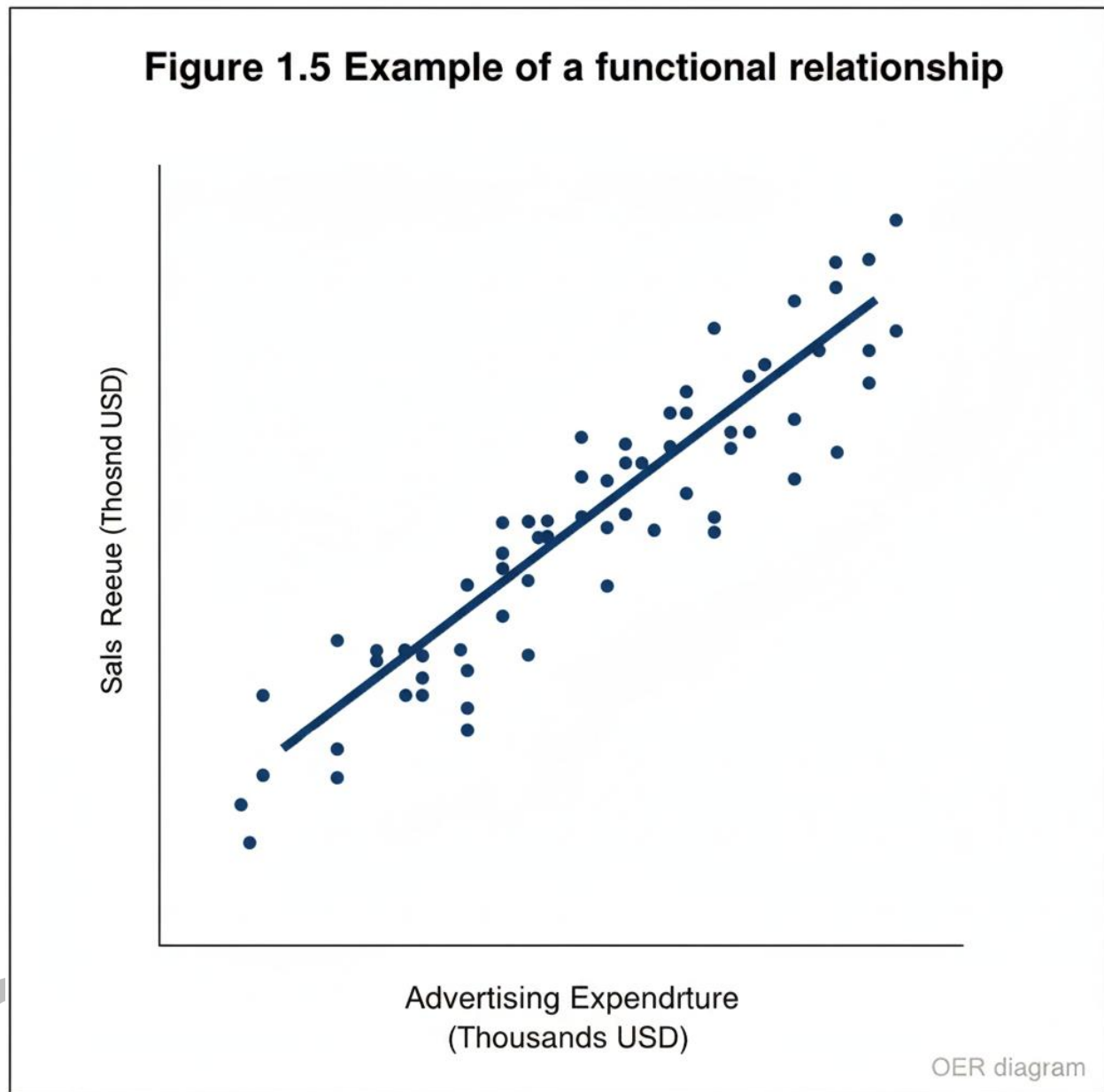
OER diagram

#### 1.4.2 Functional relationships in statistics



A **functional relationship** describes how one variable changes in response to another. For example, sales revenue may increase as advertising expenditure increases. These relationships can be expressed mathematically, often using equations or graphs, to show the connection between dependent and independent variables.

Fill in the blank: A functional relationship shows how one variable changes in response to another \_\_\_\_\_.



#### 1.4.3 Sources of statistical data

**Sources of data** refer to the origins from which information is collected for statistical analysis. Data can be obtained from **primary sources**, such as surveys, interviews, and experiments, or from **secondary sources**, such as published reports, government records, and company



databases. The choice of source depends on the purpose of the inquiry and the resources available.

Fill in the blank: Surveys and interviews are examples of \_\_\_\_\_ sources of data, while published reports are secondary sources.

### **Box 1.3 Examples of primary and secondary sources of data**

#### **Primary Sources**

- Surveys
- Interviews
- Experiments
- Reports
- Records
- Databases

OER summary

#### **Pilot questions 1.4**

1. What is the difference between discrete and continuous variables?
2. Fill in the blank: A functional relationship shows how one variable changes in response to another \_\_\_\_\_.
3. Give one example of a functional relationship in business.
4. What are primary sources of data?



5. Fill in the blank: Surveys and interviews are examples of \_\_\_\_\_ sources of data.

## Series summary

This Series has introduced you to the foundations and role of business statistics, highlighting its importance as a tool for evidence-based decision-making. We began by exploring the nature and scope of statistics, including its definition, branches, and relevance to business performance. We then examined statistical inquiries, their forms, design, and limitations, before moving on to the role of statistics in business and economics, where applications in performance measurement, market surveys, and ethical practice were discussed. Finally, we considered basic concepts such as variables, functional relationships, and sources of data.

By working through these Parts, you should now be able to define statistics and distinguish between its branches, explain its importance in business decision-making, identify and design statistical inquiries, evaluate their limitations, and discuss ethical considerations. You should also be able to differentiate between discrete and continuous variables, explain functional relationships, and classify sources of data. These abilities directly reflect the Series Learning Outcomes and provide you with a strong foundation for the more technical topics that follow in later Series.

## Glossary of terms

- **Descriptive statistics:** The branch of statistics that summarises and presents data using measures such as averages, percentages, charts, and graphs.
- **Discrete variable:** A variable that takes distinct, separate values, often whole numbers, such as the number of employees.
- **Ethical considerations:** Principles of honesty, fairness, transparency, and confidentiality that guide the proper use of statistics.
- **Functional relationship:** A connection showing how one variable changes in response to another, often expressed mathematically or graphically.
- **Inferential statistics:** The branch of statistics that uses sample data to make generalisations or predictions about a larger population.
- **Market survey:** An investigation conducted to gather information about consumer preferences, buying habits, and product demand.
- **Primary source of data:** Information collected directly from original sources such as surveys, interviews, or experiments.
- **Secondary source of data:** Information obtained from existing records or publications such as reports, government documents, or databases.
- **Statistics:** The science of collecting, organising, analysing, and interpreting data to support decision-making.



- **Variable:** Any characteristic or attribute that can take different values, classified as discrete or continuous.

## Concept Check Questions [Series 1]

### Objective questions

1. Which branch of statistics summarises and presents data? (Linked to SLO 2.1)
2. A variable that can take any value within a given range is called a \_\_\_\_\_ variable. (Linked to SLO 2.7)
3. Which type of statistical inquiry collects data from the entire population? (Linked to SLO 2.3)
4. Ethical practice in statistics requires respect for the \_\_\_\_\_ of respondents. (Linked to SLO 2.6)
5. Which source of data involves information collected directly from surveys and interviews? (Linked to SLO 2.9)

### Short-answer questions

6. Define inferential statistics and explain its purpose. (Linked to SLO 2.1)
7. Identify one limitation of statistical inquiries in business research. (Linked to SLO 2.4)
8. Explain the importance of statistics in business decision-making. (Linked to SLO 2.2)
9. Give one example of a functional relationship in business. (Linked to SLO 2.8)
10. List two examples of secondary sources of data. (Linked to SLO 2.9)

### Long-answer questions

11. Analyse the role of statistics in business performance measurement, giving examples of tools and applications. (Linked to SLO 2.5)
12. Evaluate the ethical considerations in statistical practice and discuss their impact on business research. (Linked to SLO 2.6)

## Answers to Concept Check Questions [Series 1]

### Objective questions

1. Descriptive statistics.
2. Continuous variable.
3. Census inquiry.
4. Confidentiality.
5. Primary source of data.



### Short-answer questions

6. Inferential statistics uses sample data to make generalisations or predictions about a larger population. Its purpose is to draw conclusions beyond the immediate data set.
7. One limitation is biased sampling, which can lead to misleading results.
8. Statistics helps managers make evidence-based decisions by providing insights into performance, demand, and risk.
9. An example is the relationship between advertising expenditure and sales revenue.
10. Published reports and government records.

### Long-answer questions

11. *Basic response:* Statistics measures business performance using tools such as averages, ratios, and trend analysis. For example, monthly sales figures can be compared to identify growth patterns. *Value-added response:* Beyond these basics, statistics supports forecasting, benchmarking, and risk analysis. Advanced tools such as regression models allow businesses to predict future performance based on historical data, while index numbers help track changes in costs or productivity over time.
12. *Basic response:* Ethical considerations include honesty, fairness, transparency, and confidentiality. They ensure that data is collected and reported accurately. *Value-added response:* In practice, ethical issues affect trust and credibility in business research. Misrepresentation of data or selective reporting can damage reputations and lead to poor decisions. Ethical compliance also aligns with legal standards and promotes sustainable business practices.

## Answers to Pilot Questions [Series 1]

### Part 1.1

1. Descriptive statistics.
2. Inferential statistics.
3. To provide evidence-based insights for decision-making.
4. Organising.
5. By analysing sales data to identify trends.

### Part 1.2

1. Census inquiry collects data from the whole population, while sample inquiry collects from a subset.
2. Defining the problem.
3. Because it ensures reliable and valid results.
4. Emotions.



5. Limited representativeness of surveys.

### **Part 1.3**

1. Ratios, averages, and trend analysis.
2. To gather information about consumer preferences and product demand.
3. Preferences.
4. They prevent misrepresentation and promote fairness and transparency.
5. Selective reporting of favourable results.

### **Part 1.4**

1. Discrete variables take distinct values, while continuous variables can take any value within a range.
2. Another variable.
3. Sales revenue increasing with advertising expenditure.
4. Data collected directly from original sources such as surveys.
5. Primary.

## **Series 2: Data Collection, Presentation, and Analysis Techniques**

### **Series outline**

- **Part 2.1 Sources of Data**
  - 2.1.1 Primary sources of data
  - 2.1.2 Secondary sources of data
  - 2.1.3 Choosing appropriate sources for business research
- **Part 2.2 Methods of Collecting Primary Data**
  - 2.2.1 Surveys and questionnaires
  - 2.2.2 Interviews and observations
  - 2.2.3 Experiments and case studies
- **Part 2.3 Presentation of Statistical Data**
  - 2.3.1 Tabular presentation
  - 2.3.2 Graphical presentation (charts, diagrams, histograms)
  - 2.3.3 Textual presentation
- **Part 2.4 Techniques of Data Analysis**
  - 2.4.1 Frequency distributions
  - 2.4.2 Cross-tabulation and classification



- 2.4.3 Use of summary measures in analysis

# Introduction

In business research, data is the foundation upon which decisions are built. Without reliable data, managers and researchers would struggle to identify trends, measure performance, or design strategies. This Series focuses on how data is sourced, collected, presented, and analysed, ensuring that you gain the skills to handle information in a structured and meaningful way.

The aim of this Series is to equip you with the knowledge and techniques required to collect data effectively, present it clearly, and apply basic analysis methods that support business decision-making.

We shall commence this Series by examining the sources of data, distinguishing between primary and secondary sources, and considering how to select the most appropriate ones for business research. Next, we will explore methods of collecting primary data, including surveys, interviews, observations, and experiments. Following that, we will move on to the presentation of statistical data, where you will learn how to use tables, charts, and textual formats to communicate findings. Finally, we will conclude with techniques of data analysis, focusing on frequency distributions, classification, and summary measures that help interpret data meaningfully.

## Series Learning Outcomes

Upon completing this Series, you should be able to:

- 2.1 define primary and secondary sources of data,
- 2.2 explain how to select appropriate sources of data for business research,
- 2.3 describe methods of collecting primary data such as surveys, interviews, observations, and experiments,
- 2.4 demonstrate how to present statistical data using tabular formats,
- 2.5 construct graphical presentations of data including charts, diagrams, and histograms,
- 2.6 apply textual presentation techniques to communicate statistical findings clearly,
- 2.7 organise data into frequency distributions for analysis,
- 2.8 analyse data using cross-tabulation and classification methods, and
- 2.9 apply summary measures to interpret business data effectively.

## 2.1 Sources of Data

### 2.1.1 Primary sources of data

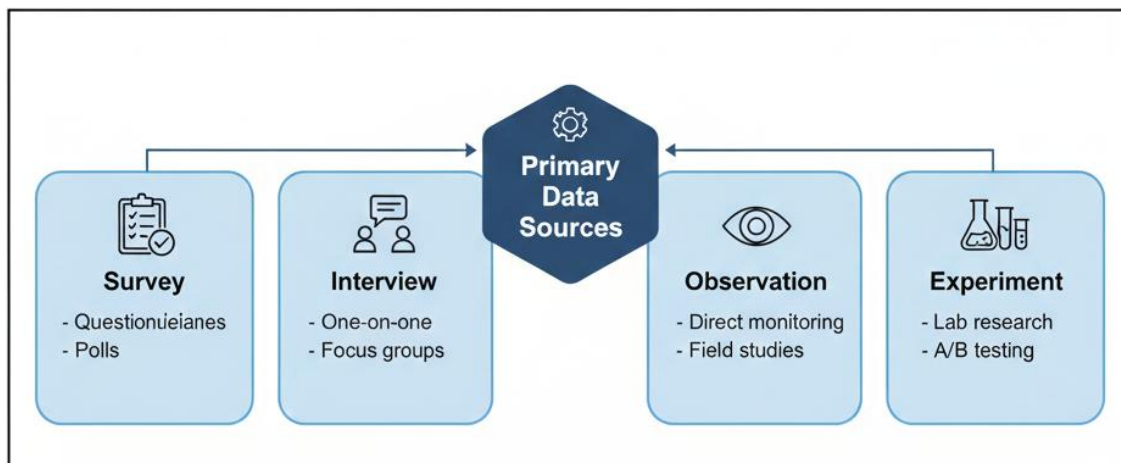
**Primary sources of data** are those obtained directly from original investigations. They involve collecting information first-hand through methods such as surveys, interviews, observations, and



experiments. These sources are particularly valuable because they provide fresh, specific, and relevant information tailored to the objectives of the research. For example, a business may conduct a customer satisfaction survey to gather direct feedback from its clients.

Fill in the blank: Surveys, interviews, and experiments are examples of \_\_\_\_\_ sources of data.

**Figure 2.1 Examples of Primary Sources of Data**



OER diagram

### 2.1.2 Secondary sources of data

**Secondary sources of data** are those collected by someone else but used for analysis in a new context. They include published reports, government records, company databases, and academic publications. These sources are often easier to access and less costly than primary data, but they may not always be perfectly aligned with the specific needs of the research. For instance, a business analyst may use government trade statistics to evaluate market trends.



Fill in the blank: Published reports and government records are examples of \_\_\_\_\_ sources of data.

**Table 2.1 Comparison of primary secondary sources of data**

| Characteristic | Primary Sources                                    | Secondary Sources                                        |
|----------------|----------------------------------------------------|----------------------------------------------------------|
| Definition     | New, original data collected firsthand             | Existing data collected by others for different purposes |
| Examples       | Surveys, Interviews, Experiments, Observations     | Reports, Records, Databases, Publications                |
| Advantages     | Tailored to needs, Higher control, More up-to-date | Cost-effective, Time-saving, Wide availability           |

OER table

### 2.1.3 Choosing appropriate sources for business research

Selecting the right source of data depends on the purpose of the research, the resources available, and the level of accuracy required. Primary data is best when specific and current information is needed, while secondary data is useful for background studies or when time and cost constraints exist. A balanced approach often involves combining both sources to achieve comprehensive results.

Fill in the blank: Primary data is best when specific and \_\_\_\_\_ information is required.



## **Box 2.1 Guidelines for choosing appropriate sources of data**

- Purpose of research
- Cost considerations
- Accuracy requirements
- Time constraints

OER summary

### **Pilot questions 2.1**

1. What are primary sources of data?
2. Give two examples of secondary sources of data.
3. Fill in the blank: Surveys, interviews, and experiments are examples of \_\_\_\_\_ sources of data.
4. Why might secondary data be less costly than primary data?
5. What factors should be considered when choosing appropriate sources of data for business research?



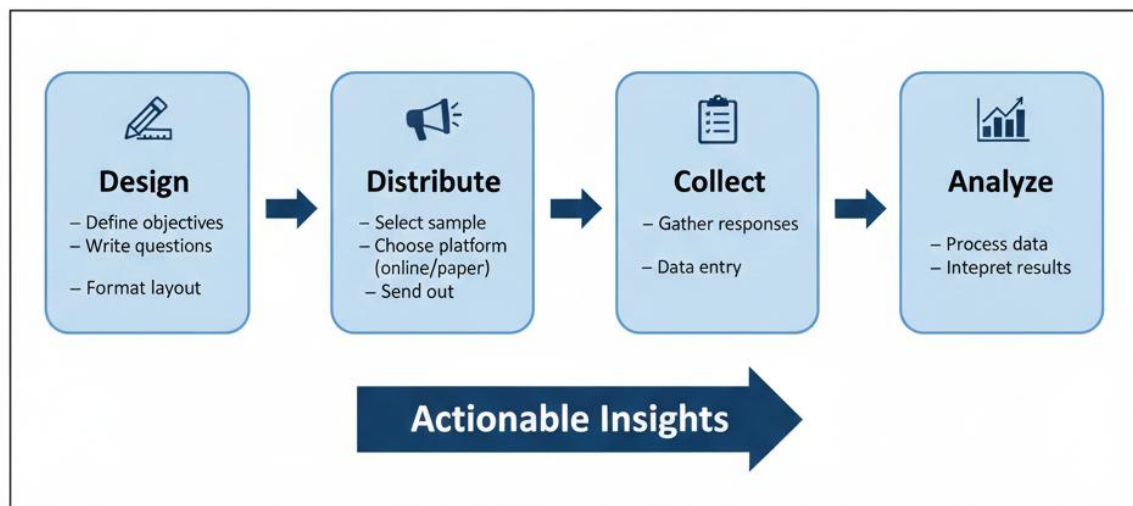
## 2.2 Methods of Collecting Primary Data

### 2.2.1 Surveys and questionnaires

**Surveys** are structured investigations where information is collected from a group of respondents using a set of questions. **Questionnaires** are written instruments used in surveys to gather responses systematically. These methods are widely used in business research because they allow for the collection of large amounts of data in a relatively short time. For example, a company may distribute questionnaires to customers to assess satisfaction levels.

Fill in the blank: Questionnaires are written instruments used in \_\_\_\_\_ to gather responses systematically.

**Figure 2.2 Process of conducting surveys and questionnaires**



OER diagram

### 2.2.2 Interviews and observations



**Interviews** involve direct interaction between the researcher and the respondent, allowing for deeper insights into opinions and experiences. They can be structured, semi-structured, or unstructured depending on the level of flexibility required. **Observations** involve watching and recording behaviours or events as they occur naturally. For instance, a retailer may observe customer movement patterns in a store to improve layout design.

Fill in the blank: Interviews can be structured, semi-structured, or \_\_\_\_\_ depending on flexibility required.



Plate 2.1 Conducting interviews for primary data collection OER image

### 2.2.3 Experiments and case studies



**Experiments** are controlled investigations where variables are manipulated to observe their effects. They are useful in testing cause-and-effect relationships. For example, a business may experiment with different pricing strategies to see how they affect sales. **Case studies** involve an in-depth examination of a single entity, such as a company or project, to draw detailed insights. They provide rich qualitative data that complements other methods.

Fill in the blank: Experiments are controlled investigations where \_\_\_\_\_ are manipulated to observe their effects.

### **Box 2.2 Examples of experiments and case studies in business research**

- Pricing experiments
- Advertising impact studies
- Company case studies

OER summary

#### **Pilot questions 2.2**

1. What is the main purpose of questionnaires in surveys?
2. Fill in the blank: Interviews can be structured, semi-structured, or \_\_\_\_\_.



3. Give one example of how observation can be used in business research.
4. What is the key feature of experiments in data collection?
5. Give one example of a case study in business research.

## 2.3 Presentation of Statistical Data

### 2.3.1 Tabular presentation

**Tabular presentation** refers to the arrangement of data in rows and columns, making it easier to read and interpret. Tables are particularly useful when dealing with large datasets, as they allow for systematic organisation and comparison. For example, a company may present monthly sales figures in a table to highlight variations across different regions.

Fill in the blank: Tabular presentation arranges data in \_\_\_\_\_ and columns for easier interpretation.



**Table 2.2 Example of tabular presentation of monthly sales data**

|          | Region A<br>(USD) | Region B<br>(USD) | Region C<br>(USD) |
|----------|-------------------|-------------------|-------------------|
| Month    |                   |                   |                   |
|          | 15,000            | 10,000            | 7,000             |
| January  | 18,000            | 12,000            | 8,500             |
| February | 20,000            | 11,000            | 9,000             |
| March    | 20,000            | 11,000            | 10,000            |
| April    | 22,000            | 13,500            | 10,000            |
| May      | 25,000            | 14,000            | 11,200            |
| June     | 28,000            | 15,500            | 12,500            |

OER table

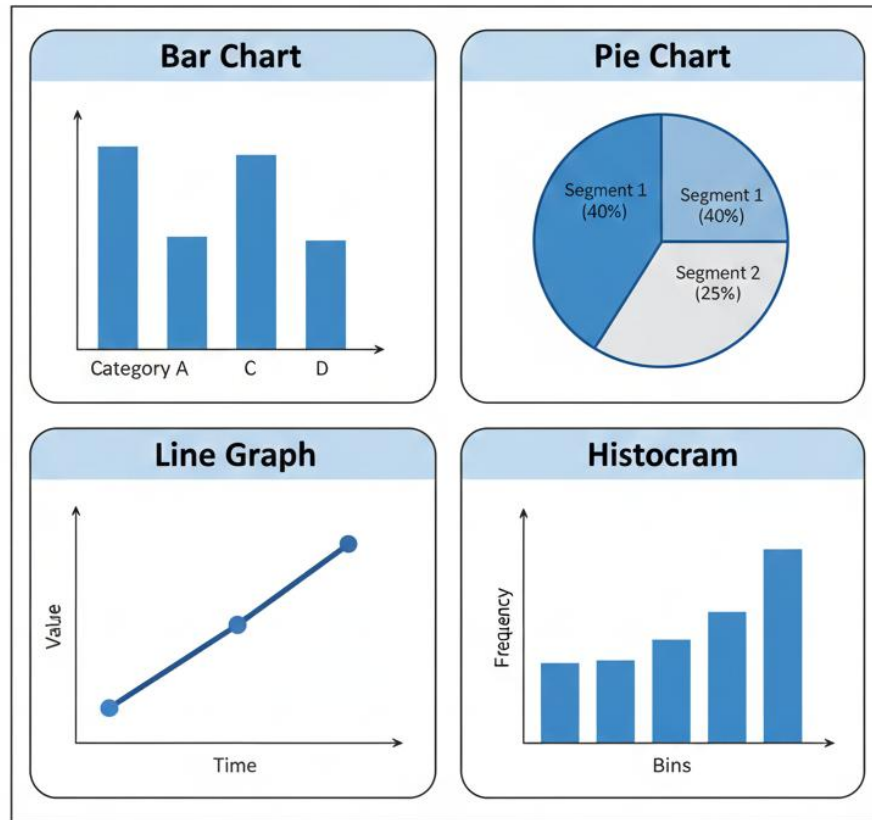
### 2.3.2 Graphical presentation (charts, diagrams, histograms)

**Graphical presentation** involves representing data visually using charts, diagrams, or histograms. This method makes patterns and trends more apparent and easier to communicate. Common forms include bar charts, pie charts, line graphs, and histograms. For instance, a bar chart may be used to compare product sales, while a pie chart can show market share distribution.

Fill in the blank: A \_\_\_\_\_ chart is often used to show market share distribution.



Figure 2.3 Common types of graphical presentation



OER diagram

### 2.3.3 Textual presentation

**Textual presentation** refers to the use of descriptive statements to explain data findings. It is often used when the dataset is small or when the emphasis is on interpretation rather than numbers. For example, a manager may write a report stating that sales increased steadily over the last quarter, without including detailed figures.

Fill in the blank: Textual presentation uses descriptive \_\_\_\_\_ to explain data findings.



### Box 2.3 Guidelines for effective textual presentation

- **Clarity:** Use simple, precise language
- **Conciseness:** Avoid jargon and unnecessary details
- **Relevance:** Focus, key findings and insights
- **Accuracy:** Ensure facts and figures are correct
- **Coherence:** Organize information logically

OER summary

#### Pilot questions 2.3

1. What is the main advantage of tabular presentation?
2. Fill in the blank: A \_\_\_\_\_ chart is often used to show market share distribution.
3. Give one example of when textual presentation may be more appropriate than tabular presentation.
4. What are two common forms of graphical presentation?
5. Why is graphical presentation often preferred when communicating trends?

#### 2.4 Techniques of Data Analysis



### 2.4.1 Frequency distributions

A **frequency distribution** is a way of organising data to show how often each value occurs. It helps to simplify large datasets and highlight patterns. For example, a business may use a frequency distribution to show how many customers fall into different age groups.

Fill in the blank: A frequency distribution shows how often each \_\_\_\_\_ occurs in a dataset.

**Table 2.3 Example of a frequency distribution of customer age groups**

| Age Group | Number of Customers (Frequency) | Percentage of Customers |
|-----------|---------------------------------|-------------------------|
| Under 25  | 120                             | 24%                     |
| 25-44     | 250                             | 18%                     |
| 45-6+     | 90                              | 8%                      |

OER table

### 2.4.2 Cross-tabulation and classification

**Cross-tabulation** is a method of analysing data by comparing two or more variables in a table format. It helps identify relationships and patterns. For instance, a retailer may cross-tabulate



customer age with product preference. **Classification** involves grouping data into categories based on shared characteristics, making it easier to interpret.

Fill in the blank: Cross-tabulation compares two or more \_\_\_\_\_ in a table format.

Figure 2.4 Example of cross-tabulation in business research

| Customer  |           | Product Preference (A, B C) |           |             |
|-----------|-----------|-----------------------------|-----------|-------------|
| Age Group |           | Product A                   | Product B | Product C   |
| Under 25  | 120 (48%) | 80 (32%)                    | 50 (30%)  | 320 (12%)   |
| Under 25  | 80 (32%)  | 80 (40%)                    | 20 (40%)  | 50 (20%)    |
| 25-44     | 150 (30%) | 200 (40%)                   | 150 (40%) | 70 (35%)    |
| 45-6+     | 50 (25%)  | 80 (35%)                    | 70 (45%)  |             |
| Total     |           |                             |           | 1000 (100%) |

OER diagram

#### 2.4.3 Use of summary measures in analysis

**Summary measures** are statistical values that describe a dataset in a concise way. Common measures include the mean (average), median (middle value), and mode (most frequent value). These measures help businesses interpret data quickly and make decisions. For example, the mean sales figure may be used to assess overall performance, while the mode may highlight the most popular product.

Fill in the blank: The mean, median, and mode are examples of \_\_\_\_\_ measures.



## Box 2.4 Common summary measures in business data analysis

- **Mean:** Average value; used for performance tracking and forecasting.
- **Median:** Middle value; useful for skewed data like salaries or salaries or property prices.
- **Mode**  
Most frequent value; used for product popularity or customer preferences

OER summary

### Pilot questions 2.4

1. What is the purpose of a frequency distribution?
2. Fill in the blank: Cross-tabulation compares two or more \_\_\_\_\_ in a table format.
3. Give one example of how classification can be used in business research.
4. What are the three common summary measures?
5. Why are summary measures useful in business decision-making?

### Series summary



This Series has guided you through the essential processes of working with data in business research. We began by examining sources of data, distinguishing between primary and secondary, and considering how to select the most appropriate ones. We then explored methods of collecting primary data, including surveys, interviews, observations, experiments, and case studies. From there, we moved into the presentation of statistical data, learning how to communicate findings through tables, charts, diagrams, and textual formats. Finally, we studied techniques of data analysis, focusing on frequency distributions, cross-tabulation, classification, and summary measures.

By completing this Series, you should now be able to define and explain different sources of data, describe and apply methods of primary data collection, demonstrate effective presentation techniques, and analyse data using basic statistical tools. These abilities directly reflect the Series Learning Outcomes and provide you with practical skills for handling information in business contexts.

## Glossary of terms

- **Case study:** An in-depth examination of a single entity, such as a company or project, to gain detailed insights.
- **Classification:** Grouping data into categories based on shared characteristics to simplify interpretation.
- **Cross-tabulation:** A method of comparing two or more variables in a table format to identify relationships.
- **Experiment:** A controlled investigation where variables are manipulated to observe their effects.
- **Frequency distribution:** An arrangement of data showing how often each value occurs.
- **Graphical presentation:** Visual representation of data using charts, diagrams, or histograms.
- **Primary source of data:** Information collected directly from original sources such as surveys, interviews, or observations.
- **Questionnaire:** A written instrument used in surveys to collect responses systematically.
- **Secondary source of data:** Information obtained from existing records or publications such as reports or databases.
- **Summary measures:** Statistical values such as mean, median, and mode that describe a dataset concisely.
- **Survey:** A structured investigation where information is collected from respondents using questions.
- **Tabular presentation:** Arrangement of data in rows and columns for systematic organisation and comparison.



- **Textual presentation:** Use of descriptive statements to explain data findings without detailed figures.

## Concept Check Questions [Series 2]

### Objective questions

1. Which type of data source involves collecting information directly from original investigations? (Linked to SLO 2.1)
2. Published reports and government records are examples of \_\_\_\_\_ sources of data. (Linked to SLO 2.1)
3. Which method of primary data collection uses written instruments to gather responses systematically? (Linked to SLO 2.3)
4. A bar chart, pie chart, and histogram are examples of \_\_\_\_\_ presentation. (Linked to SLO 2.5)
5. The mean, median, and mode are examples of \_\_\_\_\_ measures. (Linked to SLO 2.9)

### Short-answer questions

6. Define secondary sources of data and give one example. (Linked to SLO 2.1)
7. Explain the main advantage of using surveys in business research. (Linked to SLO 2.3)
8. Why might textual presentation be more appropriate than tabular presentation in some cases? (Linked to SLO 2.6)
9. Give one example of how cross-tabulation can be used in business research. (Linked to SLO 2.8)
10. What is the purpose of frequency distributions in data analysis? (Linked to SLO 2.7)

### Long-answer questions

11. Analyse the strengths and limitations of primary and secondary sources of data in business research. (Linked to SLO 2.2)
12. Evaluate the role of graphical presentation in communicating business data, giving examples of different chart types. (Linked to SLO 2.5)

## Answers to Concept Check Questions [Series 2]

### Objective questions

1. Primary sources of data.
2. Secondary.
3. Questionnaire.
4. Graphical.



## 5. Summary.

### Short-answer questions

6. Secondary sources of data are information collected by others and reused for new analysis. Example: government trade statistics.
7. Surveys allow researchers to collect large amounts of data quickly and systematically.
8. Textual presentation is more appropriate when datasets are small or when interpretation is more important than numbers.
9. Cross-tabulation can be used to compare customer age with product preference.
10. Frequency distributions simplify large datasets by showing how often each value occurs.

### Long-answer questions

11. *Basic response:* Primary sources provide fresh, specific data but are costly and time-consuming. Secondary sources are cheaper and easier to access but may not align perfectly with research needs. *Value-added response:* Primary sources enhance accuracy and relevance, while secondary sources provide context and background. Combining both can yield comprehensive insights, balancing cost, timeliness, and precision.
12. *Basic response:* Graphical presentation makes data easier to understand by showing patterns and trends visually. Examples include bar charts for comparisons and pie charts for proportions. *Value-added response:* Graphical tools enhance communication by simplifying complex datasets. Line graphs highlight trends over time, histograms show distributions, and pie charts illustrate market share. Effective use of these tools improves decision-making and stakeholder engagement.

## Answers to Pilot Questions [Series 2]

### Part 2.1

1. Primary sources of data are information collected directly from original investigations.
2. Published reports and government records.
3. Primary.
4. Because they are already collected and published, saving time and cost.
5. Purpose of research, cost considerations, and accuracy requirements.

### Part 2.2

1. To collect responses systematically in surveys.
2. Unstructured.
3. Observing customer movement patterns in a store.
4. Manipulation of variables to observe effects.



5. A detailed study of a company's marketing strategy.

### **Part 2.3**

1. It organises large datasets systematically for easy comparison.
2. Pie.
3. When the dataset is small and interpretation is more important than numbers.
4. Bar charts and line graphs.
5. Because they make patterns and trends more apparent.

### **Part 2.4**

1. To simplify large datasets and highlight patterns.
2. Variables.
3. Grouping customers by income levels.
4. Mean, median, and mode.
5. They provide concise summaries that aid quick decision-making.

## **Series 3: Measures of Central Tendency, Dispersion, and Probability Distributions**

### **Outline of Parts**

- **Part 3.1 Measures of Central Tendency**
  - 3.1.1 Definition and importance of central tendency
  - 3.1.2 Mean, median, and mode
  - 3.1.3 Applications of central tendency in business decision-making
- **Part 3.2 Measures of Dispersion**
  - 3.2.1 Definition and significance of dispersion
  - 3.2.2 Range, variance, and standard deviation
  - 3.2.3 Coefficient of variation and its business applications
- **Part 3.3 Probability Concepts**
  - 3.3.1 Definition of probability and its role in statistics
  - 3.3.2 Rules of probability (addition and multiplication)
  - 3.3.3 Conditional probability and independence
- **Part 3.4 Probability Distributions**
  - 3.4.1 Discrete probability distributions (binomial, Poisson)
  - 3.4.2 Continuous probability distributions (normal distribution)
  - 3.4.3 Applications of probability distributions in business and economics



## Introduction

Statistics is not only about collecting and presenting data; it is also about summarising and interpreting it in ways that support sound decision-making. In business and economics, managers often need to identify typical values, measure variability, and assess the likelihood of future events. This Series focuses on three fundamental areas: **measures of central tendency**, **measures of dispersion**, and **probability distributions**.

The aim of this Series is to equip you with the ability to calculate and interpret averages, understand the spread of data, and apply probability concepts to business situations. We begin with measures of central tendency, exploring the mean, median, and mode as ways of identifying representative values. Next, we turn to measures of dispersion, such as range, variance, and standard deviation, which help us understand how data varies around the centre. We then introduce probability concepts, including rules and conditional probability, before concluding with probability distributions, both discrete and continuous, and their applications in business decision-making.

## Series Learning Outcomes

Upon completing **Series 3**

- **3.1** define measures of central tendency and explain their importance in summarising data,
- **3.2** calculate the mean, median, and mode for different types of datasets,
- **3.3** apply measures of central tendency to business decision-making scenarios,
- **3.4** define measures of dispersion and explain their significance in understanding variability,
- **3.5** compute range, variance, and standard deviation for given datasets,
- **3.6** interpret the coefficient of variation and evaluate its applications in business research,
- **3.7** define probability and explain its role in statistical analysis,
- **3.8** apply rules of probability including addition and multiplication,
- **3.9** analyse conditional probability and independence in practical contexts,
- **3.10** distinguish between discrete and continuous probability distributions,
- **3.11** apply binomial, Poisson, and normal distributions to solve business-related problems.

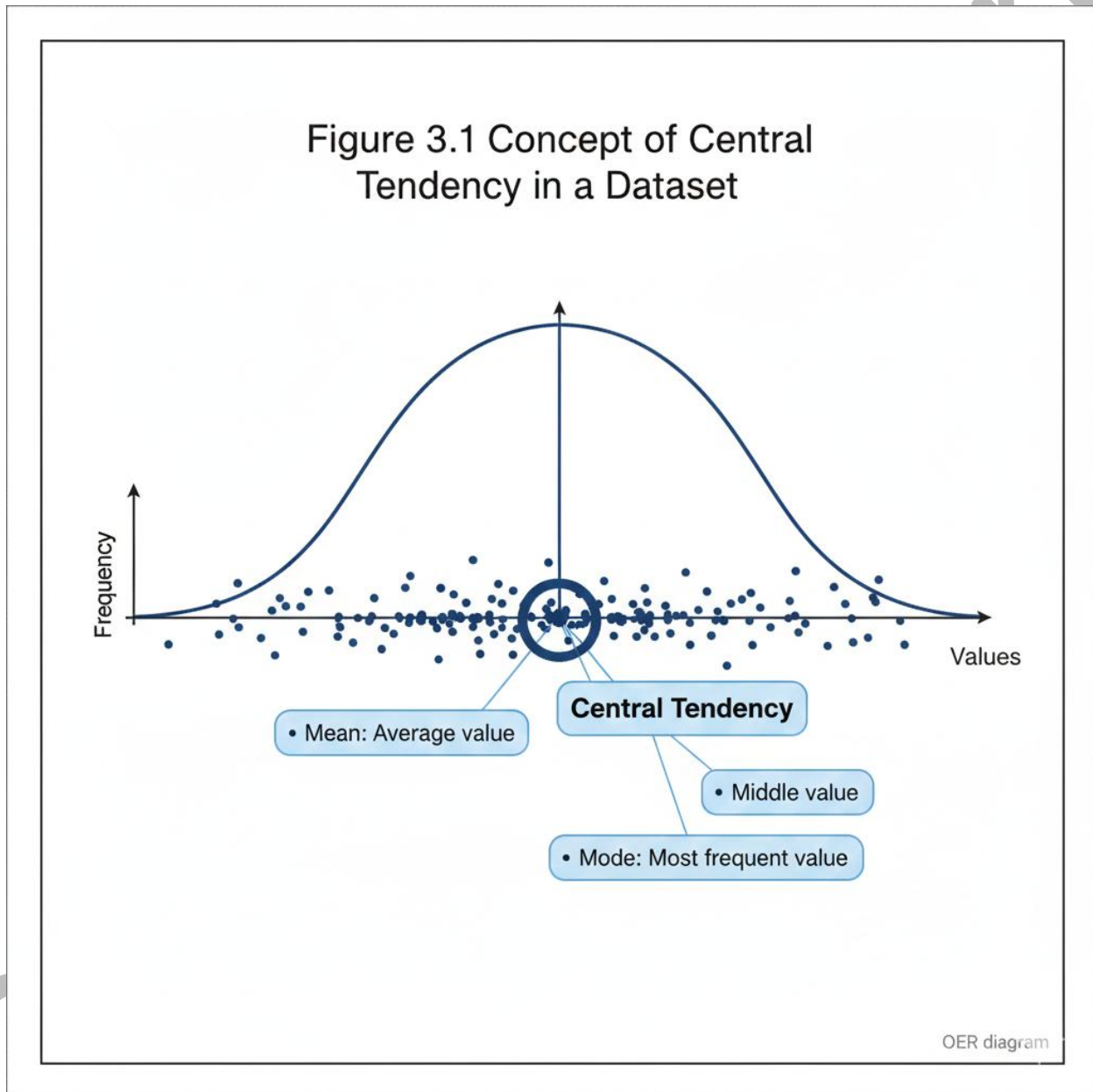
### 3.1 Measures of Central Tendency

#### 3.1.1 Definition and importance of central tendency



**Central tendency** refers to statistical measures that identify a single value representing the centre or typical point of a dataset. These measures help summarise large amounts of data into a single figure, making interpretation easier. In business, central tendency is crucial for understanding average sales, typical customer behaviour, or standard production levels.

Fill in the blank: Central tendency identifies a single value that represents the \_\_\_\_\_ of a dataset.



### 3.1.2 Mean, median, and mode

The **mean** is the arithmetic average, calculated by dividing the sum of all values by the number of values. The **median** is the middle value when data is arranged in order, and the **mode** is the most frequently occurring value. Each measure has its strengths: the mean is useful for



continuous data, the median is better when data contains extreme values, and the mode is ideal for categorical data.

Fill in the blank: The \_\_\_\_\_ is the most frequently occurring value in a dataset.

**Table 3.1 Comparison of mean, median, and mode**

| Characteristic                       | Mean                                             | Median                              | Mode                         |
|--------------------------------------|--------------------------------------------------|-------------------------------------|------------------------------|
| Definition                           | Average value                                    | Middle value when ordered           | Most frequent value          |
| Calculation                          | Sum of all values / Number of ( $\Sigma x / n$ ) | Middle value(s) of sorted data      | Value with highest frequency |
| Symmetric data, performance tracking |                                                  | Skewed data, income/property prices | Categorical data, popularity |

OER table

### 3.1.3 Applications of central tendency in business decision-making

Central tendency measures are widely applied in business. For example, the mean can be used to calculate average monthly sales, the median can identify the typical income level of customers, and the mode can highlight the most popular product in a store. These applications help managers make informed decisions about pricing, marketing, and resource allocation.

Fill in the blank: The median is useful for identifying the \_\_\_\_\_ income level of customers.



## Box 3.1 Applications of central tendency in business

- **Average Sales:** Tracking performance and setting targets
- **Typical Income:** Market segmentation and compensation analysis
- **Popular Product Identification:** Inventory
- **Popular Product management and marketing strategy**
- **Customer Lifetime Value (CLTV):**  
Predicting profitability and resource allocation

OER summary

### Pilot questions 3.1

1. What does central tendency measure in a dataset?
2. Fill in the blank: The \_\_\_\_\_ is the most frequently occurring value in a dataset.
3. Give one example of when the median is more useful than the mean.
4. What is the main advantage of using the mean in continuous data?
5. How can the mode be applied in business decision-making?

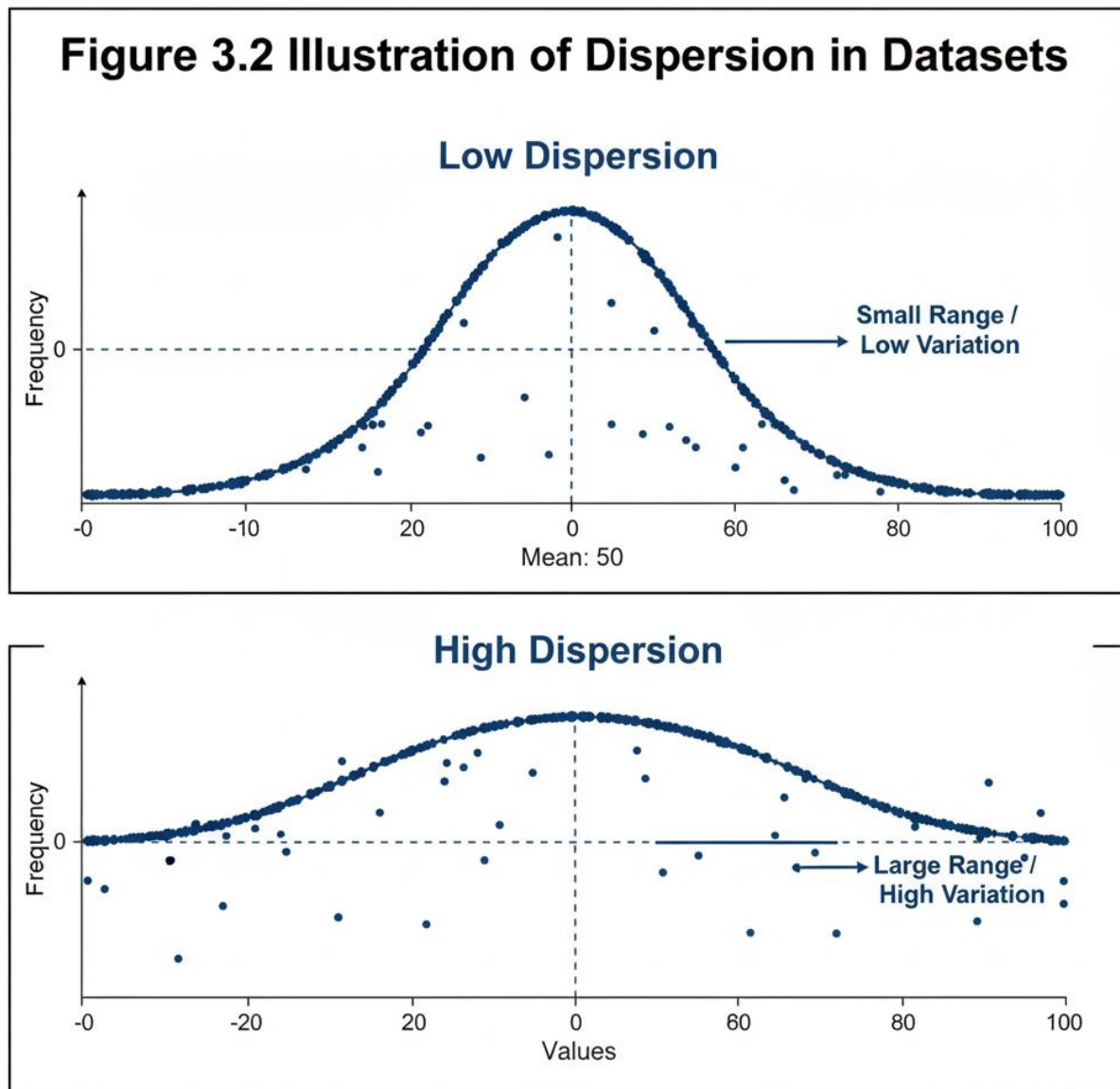
### 3.2 Measures of Dispersion

#### 3.2.1 Definition and significance of dispersion



**Dispersion** refers to the extent to which data values are spread out around a central point. While measures of central tendency summarise data with a single representative value, dispersion shows how much variation exists. In business, dispersion is important because it highlights risk, consistency, and reliability. For example, two products may have the same average sales, but if one has highly variable sales and the other is stable, managers will make very different decisions.

Fill in the blank: Dispersion shows how much \_\_\_\_\_ exists around a central point in a dataset.



OER diagram

### 3.2.2 Range, variance, and standard deviation

The **range** is the simplest measure of dispersion, calculated as the difference between the highest and lowest values. **Variance** measures the average squared deviation from the mean, while



**standard deviation** is the square root of variance, showing how much values typically differ from the mean. These measures are widely used in business to assess risk and variability.

Fill in the blank: The standard deviation is the square root of \_\_\_\_\_.

**Table 3.2 Comparison of range, variance, and standard deviation**

|                    | Range                                 | Variance                                 | Standard Deviation                    |
|--------------------|---------------------------------------|------------------------------------------|---------------------------------------|
| <b>Definition</b>  | Difference between max and min values | Max Value - Min Value                    | Square root of the the Variance       |
| <b>Calculation</b> | Max Value of spread                   | Average of squared differences from Mean | Risk assessment, quality control      |
|                    | Quick measure of spread               | Data spread around the mean              | $\sqrt{\frac{\sum (x_i - \mu)^2}{n}}$ |
| <b>Application</b> |                                       | $\frac{\sum (x_i - \mu)^2}{n}$           | $\sqrt{\sum (x_i - \mu)^2 / n}$       |

OER table

### 3.2.3 Coefficient of variation and its business applications

The **coefficient of variation (CV)** is a relative measure of dispersion, calculated as the ratio of the standard deviation to the mean, often expressed as a percentage. It allows comparison of variability across datasets with different units or scales. In business, CV is useful for comparing investment risks, product performance, or operational consistency.



Fill in the blank: The coefficient of variation is calculated as the ratio of standard deviation to the \_\_\_\_\_.

## Box 3.2 Applications of coefficient of variation in business

- **Comparing Investment Risks:** Evaluate the volatility of different stocks or portfolios relative to their expected returns
- **Analyzing Product Performance:**  
Assess the consistency of product quality or sales performance across various items
- **Monitoring Operational Consistency:**  
Measure the consistency: the reliability of machinery of manufacturing processes or service delivery times

OER summary

### Pilot questions 3.2

1. What does dispersion measure in a dataset?
2. Fill in the blank: The standard deviation is the square root of \_\_\_\_\_.
3. Give one example of how range can be used in business.
4. Why is variance considered a more reliable measure than range?
5. What is the main purpose of the coefficient of variation in business analysis?



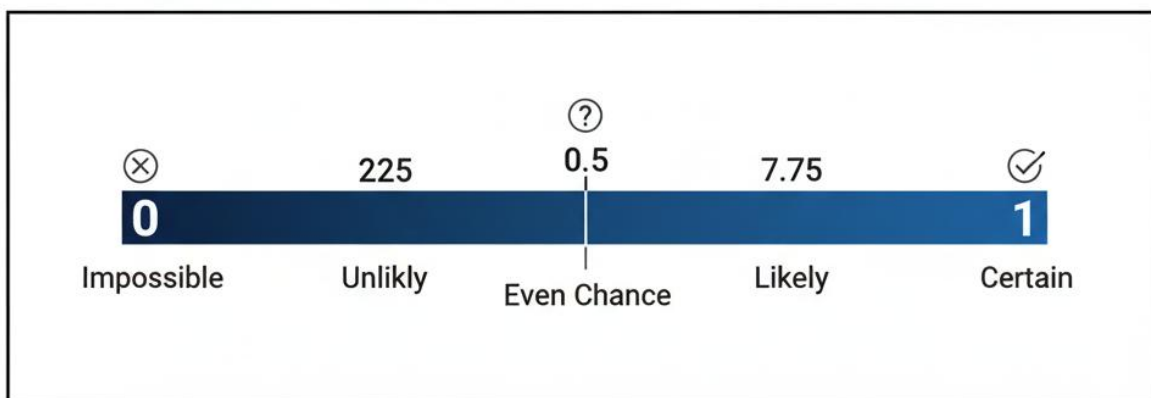
### 3.3 Probability Concepts

#### 3.3.1 Definition of probability and its role in statistics

**Probability** is the measure of the likelihood that a particular event will occur, expressed as a value between 0 and 1. A probability of 0 means the event is impossible, while a probability of 1 means it is certain. In statistics, probability provides the foundation for making predictions and assessing risk. In business, probability helps managers evaluate uncertainties such as market demand, investment returns, or customer behaviour.

Fill in the blank: A probability of 0 means an event is \_\_\_\_\_, while a probability of 1 means it is certain.

Figure 3.3 Probability scale from impossible to certain



OER diagram

#### 3.3.2 Rules of probability (addition and multiplication)



The **addition rule** is used when calculating the probability of either of two mutually exclusive events occurring. For example, the probability of drawing either a red card or a black card from a deck. The **multiplication rule** is used when calculating the probability of two independent events occurring together. For instance, the probability of rolling a 4 on a die and flipping a head on a coin.

Fill in the blank: The addition rule is used for mutually \_\_\_\_\_ events, while the multiplication rule is used for independent events.

**Table 3.3**  
**Rules of Probability**

| Rule                       | Description                                                                        | Example                                                                                                                         |
|----------------------------|------------------------------------------------------------------------------------|---------------------------------------------------------------------------------------------------------------------------------|
|                            | Probability of either event A or event B occurring (for mutually exclusive events) | $P(\text{drawing a heart or a diamond}) = P(\text{Heart}) + P(\text{Diamond}) = \frac{14}{14} + \frac{1}{12} = \frac{1}{4}$     |
| <b>Multiplication Rule</b> |                                                                                    |                                                                                                                                 |
|                            | Probability of both event A and B occurring (for independent events)               | $P(\text{flipping heads and rolling a 6}) = P(\text{Heads}) + P(\text{Rolling a 6}) = \frac{1}{2} + \frac{1}{6} = \frac{1}{12}$ |

OER table

### 3.3.3 Conditional probability and independence

**Conditional probability** is the probability of an event occurring given that another event has already occurred. For example, the probability that a customer buys a product given that they



have received a discount. **Independence** means that the occurrence of one event does not affect the probability of another. Understanding these concepts is essential in business research, especially when analysing customer behaviour or market trends.

Fill in the blank: Conditional probability is the probability of an event occurring given that another event has already \_\_\_\_\_.

### Box 3.3 Examples of conditional probability in business

- **Customer Purchase Given Discount:**

The likelihood a customer buys a product increases if offered a discount.

- **Loan Repayment Given Employment Status**

The probability of the loan being repaid is higher if the borrower is employed.

- **Project Success Given Team Experience**

The chance of a project succeeding is greater if the team has prior experience.

OER summary

#### Pilot questions 3.3

1. What does probability measure in statistics?
2. Fill in the blank: The addition rule is used for mutually \_\_\_\_\_ events.
3. Give one example of how the multiplication rule can be applied.
4. What is conditional probability?



5. Why is independence important in probability analysis?

### 3.4 Probability Distributions

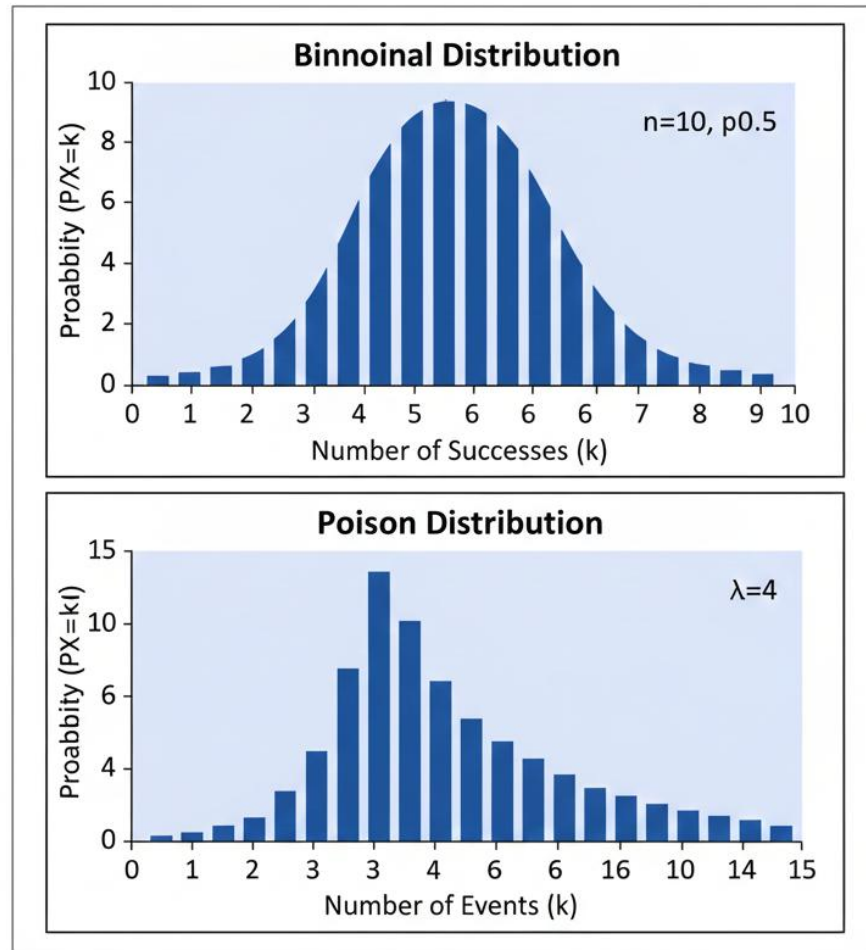
#### 3.4.1 Discrete probability distributions (binomial, Poisson)

A **discrete probability distribution** describes the likelihood of outcomes for variables that take distinct, separate values. Two common types are the **binomial distribution**, which models the probability of success in a fixed number of trials, and the **Poisson distribution**, which models the probability of a given number of events occurring in a fixed interval of time or space. In business, binomial distributions can be used to estimate customer purchase likelihood, while Poisson distributions can model call centre arrivals.

Fill in the blank: The binomial distribution models the probability of \_\_\_\_\_ in a fixed number of trials.



**Figure 3.4** Examples of discrete probability distributions



OER diagram

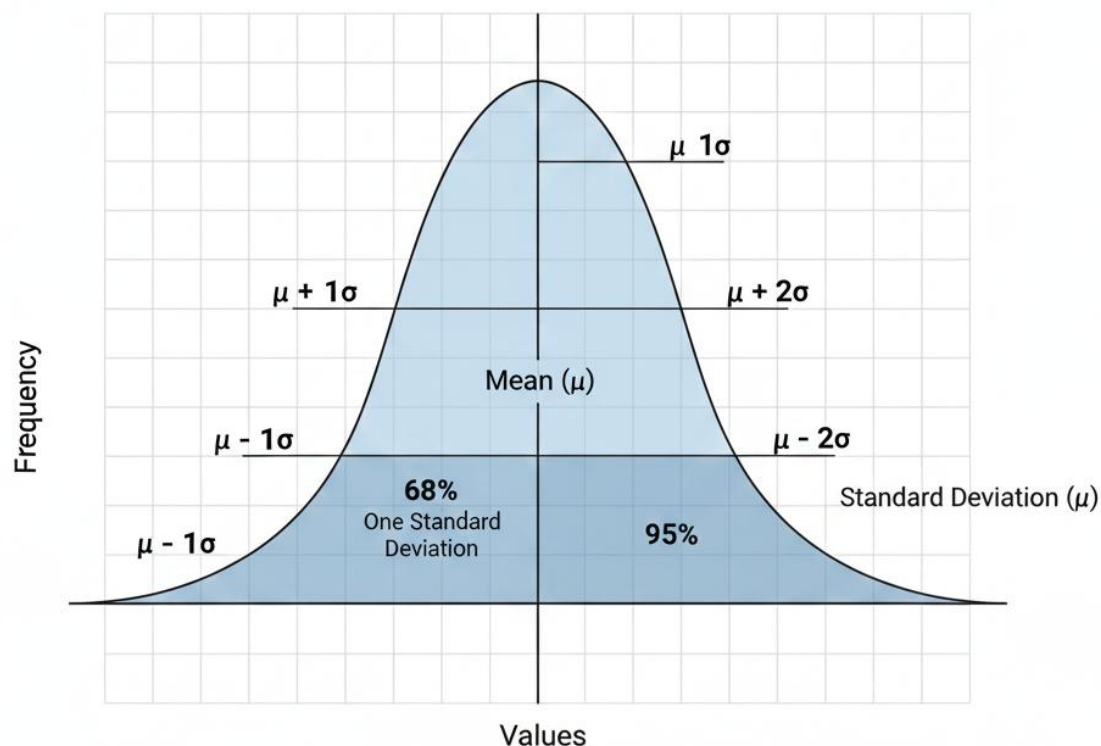
### 3.4.2 Continuous probability distributions (normal distribution)

A **continuous probability distribution** describes outcomes for variables that can take any value within a range. The most important example is the **normal distribution**, often called the bell curve, which is symmetric around the mean. Many business phenomena, such as employee performance scores or product lifespans, follow a normal distribution. Understanding this distribution is critical for forecasting and quality control.

Fill in the blank: The normal distribution is often called the \_\_\_\_\_ curve because of its shape.



## Figure 3.5 Normal distribution curve



OER diagram

### 3.4.3 Applications of probability distributions in business and economics

Probability distributions are widely applied in business decision-making. For example, binomial distributions can estimate the probability of product success, Poisson distributions can predict customer arrivals, and normal distributions can be used in quality control to assess product defects. These applications help managers plan resources, manage risks, and make evidence-based decisions.

Fill in the blank: Probability distributions help managers plan resources, manage risks, and make \_\_\_\_\_ decisions.



### BOX 3.4

#### APPLICATIONS OF PROBABILITY DISTRIBUTIONS IN BUSINESS

Probability distributions are essential tools for making informed business decisions. They help model real phenomena and predict future outcomes. Key applications include:

- **Forecasting** distributions are used to estimate product demands, inventory levels, and production schedules.
- **Forecasting Demand:** Estimating future product demand to optimize levels and production schedules.
- **Quality Control:** Monitoring manufacturing processes to ensure product quality and minimize defects (e.g., Six Sigma).
- **Risk Management:** Assessing and mitigating financial risks, such as loan defaults or market volatility. (VaR)
- **Financial Analysis:** Modeling asset returns, evaluating investment opportunities.
- **Insurance:** Determining premium rates based on predicted claim frequencies and severities.
- **Marketing Research:** Analyzing consumer behavior, predicting customer churn, and evaluating the effectiveness of marketing campaigns.

#### Pilot questions 3.4

1. What is a discrete probability distribution?
2. Fill in the blank: The normal distribution is often called the \_\_\_\_\_ curve.
3. Give one example of how the binomial distribution can be applied in business.
4. What is the main characteristic of the normal distribution?
5. Why are probability distributions important in business decision-making?

#### Series Summary



This Series introduced you to three foundational areas of statistics: **measures of central tendency**, **measures of dispersion**, and **probability distributions**. You learned how central tendency identifies representative values in a dataset through the mean, median, and mode. We then explored dispersion, which highlights variability using range, variance, standard deviation, and the coefficient of variation. Building on this, we examined probability concepts, including rules of probability, conditional probability, and independence. Finally, we studied probability distributions, both discrete (binomial, Poisson) and continuous (normal), and their applications in business decision-making.

By completing this Series, you should now be able to calculate and interpret averages, measure variability, apply probability rules, and use probability distributions to solve practical business problems.

## Glossary of Terms

- **Central tendency:** A statistical measure identifying the centre or typical value of a dataset.
- **Mean:** The arithmetic average of a dataset.
- **Median:** The middle value when data is arranged in order.
- **Mode:** The most frequently occurring value in a dataset.
- **Dispersion:** The extent to which data values are spread around a central point.
- **Range:** The difference between the highest and lowest values in a dataset.
- **Variance:** The average squared deviation from the mean.
- **Standard deviation:** The square root of variance, showing typical deviation from the mean.
- **Coefficient of variation (CV):** A relative measure of dispersion, expressed as the ratio of standard deviation to mean.
- **Probability:** The measure of likelihood that an event will occur, expressed between 0 and 1.
- **Addition rule:** Probability rule used for mutually exclusive events.
- **Multiplication rule:** Probability rule used for independent events.
- **Conditional probability:** Probability of an event occurring given that another has already occurred.
- **Independence:** When the occurrence of one event does not affect another.
- **Discrete probability distribution:** Distribution for variables with distinct values (e.g., binomial, Poisson).
- **Continuous probability distribution:** Distribution for variables with any value in a range (e.g., normal distribution).



- **Normal distribution:** A bell-shaped, symmetric distribution around the mean.

### Concept Check Questions [Series 3]

#### Objective questions

1. Which measure of central tendency is the arithmetic average? (Linked to SLO 3.2)
2. The difference between the highest and lowest values in a dataset is called the \_\_\_\_\_. (Linked to SLO 3.5)
3. The coefficient of variation is calculated as the ratio of standard deviation to the \_\_\_\_\_. (Linked to SLO 3.6)
4. The addition rule of probability is used for \_\_\_\_\_ exclusive events. (Linked to SLO 3.8)
5. The normal distribution is often referred to as the \_\_\_\_\_ curve. (Linked to SLO 3.10)

#### Short-answer questions

6. Define mode and give one example of its use in business. (Linked to SLO 3.2)
7. Explain why standard deviation is more informative than range. (Linked to SLO 3.5)
8. What is conditional probability? Give one business example. (Linked to SLO 3.9)
9. Distinguish between discrete and continuous probability distributions. (Linked to SLO 3.10)
10. Give one example of how the Poisson distribution can be applied in business. (Linked to SLO 3.11)

#### Long-answer questions

11. Analyse the strengths and limitations of mean, median, and mode in business decision-making. (Linked to SLO 3.3)
12. Evaluate the importance of probability distributions in forecasting and risk management. (Linked to SLO 3.11)

### Answers to Concept Check Questions

#### Objective Questions

1. **Mean**
2. **Range**
3. **Mean**
4. **Mutually**
5. **Bell**

#### Short-Answer Questions



6. **Mode** is the most frequently occurring value in a dataset. *Example:* In business, mode can identify the most popular product purchased by customers.
7. **Standard deviation** is more informative than range because it considers all data points, not just the extremes, giving a fuller picture of variability.
8. **Conditional probability** is the probability of an event occurring given that another event has already occurred. *Example:* The probability that a customer buys a product given that they received a discount.
9. **Discrete distributions** apply to variables with distinct, separate values (e.g., binomial, Poisson). **Continuous distributions** apply to variables that can take any value within a range (e.g., normal distribution).
10. The **Poisson distribution** can be applied to model the number of customer calls arriving at a call centre in an hour.

### Long-Answer Questions

11. **Strengths and limitations of mean, median, and mode in business decision-making:**
  - *Mean:* Easy to calculate and widely used, but sensitive to extreme values.
  - *Median:* Useful when data has outliers, but ignores the magnitude of values.
  - *Mode:* Highlights the most common category, but may be less useful with continuous data. *Overall:* Each measure has unique strengths; combining them provides a more complete picture.
12. **Importance of probability distributions in forecasting and risk management:**
  - Probability distributions help businesses predict demand, assess risks, and plan resources.
  - *Binomial:* Useful for estimating product success rates.
  - *Poisson:* Helps forecast customer arrivals or service requests.
  - *Normal:* Critical for quality control and performance analysis. *Overall:* They provide a structured way to manage uncertainty and support evidence-based decisions.

### Answers to Pilot Questions [Series 3]

#### Part 3.1

1. Central tendency measures the centre or typical value of a dataset.
2. Mode.
3. When data contains extreme values, such as income distribution.
4. It summarises continuous data into a single representative figure.
5. Identifying the most popular product in a store.



### Part 3.2

1. Dispersion measures variability around a central point.
2. Variance.
3. Comparing the highest and lowest monthly sales.
4. Because it considers all data points, not just extremes.
5. To compare variability across datasets with different scales.

### Part 3.3

1. Probability measures the likelihood of an event occurring.
2. Exclusive.
3. Rolling a die and flipping a coin simultaneously.
4. Probability of an event given another has occurred.
5. It ensures events are analysed correctly without false assumptions of dependence.

### Part 3.4

1. A distribution for variables with distinct values.
2. Bell.
3. Estimating the probability of customer purchase success.
4. Symmetry around the mean.
5. They support forecasting, risk management, and evidence-based decisions.

## Series 4: Sampling Theory, Estimation, and Hypothesis Testing

### Series Outline

- **Part 4.1 Sampling Theory**
  - 4.1.1 Definition and importance of sampling
  - 4.1.2 Types of sampling methods (random, stratified, systematic, cluster)
  - 4.1.3 Sampling errors and biases
- **Part 4.2 Estimation**
  - 4.2.1 Point estimation and properties of estimators
  - 4.2.2 Interval estimation and confidence intervals
  - 4.2.3 Applications of estimation in business research



- **Part 4.3 Hypothesis Testing: Concepts and Procedures**
  - 4.3.1 Definition and purpose of hypothesis testing
  - 4.3.2 Null and alternative hypotheses
  - 4.3.3 Type I and Type II errors
  - 4.3.4 Levels of significance and p-values
- **Part 4.4 Hypothesis Testing: Applications**
  - 4.4.1 Testing means and proportions
  - 4.4.2 Chi-square tests
  - 4.4.3 Business applications of hypothesis testing

## Introduction

Statistics is not only about describing data but also about making reliable inferences from samples. In business research, it is often impractical to collect information from an entire population, so **sampling theory** provides the framework for selecting representative subsets. Once data is collected, **estimation** techniques allow us to infer population parameters using point and interval estimates. Finally, **hypothesis testing** enables managers and researchers to make evidence-based decisions by formally evaluating claims about populations.

The aim of this Series is to equip you with the skills to design effective samples, estimate population parameters, and conduct hypothesis tests with confidence. We begin with sampling theory, exploring definitions, types of sampling methods, and common errors. Next, we move to estimation, covering point and interval estimation, along with confidence intervals. We then introduce the concepts and procedures of hypothesis testing, including null and alternative hypotheses, errors, and significance levels. Finally, we apply hypothesis testing to practical business problems such as testing means, proportions, and using chi-square tests.

By the end of this Series, you will be able to select appropriate sampling methods, perform estimation, and apply hypothesis testing to support sound business decisions.

## Series Learning Outcomes

Upon completing **Series 4**

- **4.1** define sampling and explain its importance in business research,
- **4.2** distinguish between different sampling methods such as random, stratified, systematic, and cluster sampling,
- **4.3** identify common sampling errors and biases,
- **4.4** define point estimation and describe the properties of good estimators,
- **4.5** construct interval estimates and interpret confidence intervals,
- **4.6** apply estimation techniques to business research problems,
- **4.7** define hypothesis testing and explain its purpose in statistical inference,
- **4.8** formulate null and alternative hypotheses for given scenarios,



- **4.9** distinguish between Type I and Type II errors in hypothesis testing,
- **4.10** interpret levels of significance and p-values,
- **4.11** perform hypothesis tests for means and proportions,
- **4.12** apply chi-square tests to categorical data, and
- **4.13** evaluate business decisions using hypothesis testing results.

## 4.1 Sampling Theory

### 4.1.1 Definition and importance of sampling

**Sampling** is the process of selecting a subset of individuals or items from a larger population to represent the whole. It is often impractical or impossible to study an entire population, so sampling provides a cost-effective and efficient way to gather data. In business research, sampling is crucial for market surveys, customer feedback, and product testing.

Fill in the blank: Sampling is the process of selecting a \_\_\_\_\_ of individuals or items from a population.

### 4.1.2 Types of sampling methods

There are several methods of sampling:

- **Random sampling:** Every member of the population has an equal chance of being selected.
- **Stratified sampling:** The population is divided into groups (strata), and samples are taken from each group.
- **Systematic sampling:** Selecting every nth item from a list or sequence.
- **Cluster sampling:** Dividing the population into clusters and randomly selecting entire clusters.

Fill in the blank: In \_\_\_\_\_ sampling, the population is divided into groups and samples are taken from each group.

### 4.1.3 Sampling errors and biases

**Sampling errors** occur when the sample does not perfectly represent the population, often due to chance. **Biases** occur when the sampling method systematically favours certain outcomes, such as selecting only easily accessible respondents. Minimising errors and biases is essential for reliable business research.

Fill in the blank: Sampling errors occur due to \_\_\_\_\_, while biases occur due to systematic favouring of outcomes.

#### Pilot questions 4.1

1. What is sampling in statistics?



2. Fill in the blank: In \_\_\_\_\_ sampling, every member of the population has an equal chance of being selected.
3. Give one example of stratified sampling in business research.
4. What is the difference between sampling error and bias?
5. Why is minimising sampling bias important in business decision-making?

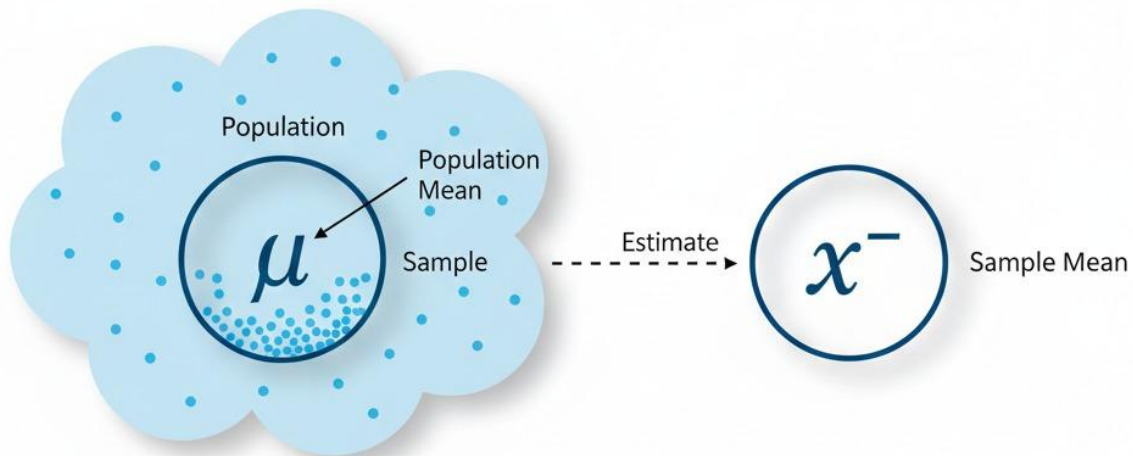
## 4.2 Estimation

### 4.2.1 Point estimation and properties of estimators

**Point estimation** involves using sample data to calculate a single value (called an estimator) that serves as the best guess of a population parameter. For example, the sample mean is often used to estimate the population mean. Good estimators should be **unbiased** (on average equal to the true parameter), **consistent** (become more accurate with larger samples), and **efficient** (have minimum variance among possible estimators).

Fill in the blank: A point estimate is a \_\_\_\_\_ value used to approximate a population parameter.





**Figure 4.2**  
Point Estimation of a Population Mean

### 4.2.2 Interval estimation and confidence intervals

**Interval estimation** provides a range of values within which the population parameter is likely to fall. A **confidence interval** expresses this range along with a confidence level (e.g., 95%), which indicates the probability that the interval contains the true parameter. In business, confidence intervals are used to estimate market share, average spending, or customer satisfaction scores with a margin of error.

Fill in the blank: A confidence interval provides a range of values within which the \_\_\_\_\_ parameter is likely to fall.

### 4.2.3 Applications of estimation in business research



Estimation techniques are widely applied in business. Point estimates can be used to approximate average customer spending, while confidence intervals can provide ranges for market demand forecasts. These tools help managers make decisions with quantified uncertainty, balancing risk and opportunity.

Fill in the blank: Confidence intervals help managers make decisions with quantified \_\_\_\_\_.

#### Pilot questions 4.2

1. What is point estimation?
2. Fill in the blank: A confidence interval provides a range of values within which the \_\_\_\_\_ parameter is likely to fall.
3. What are the properties of a good estimator?
4. Give one example of how confidence intervals can be used in business.
5. Why is interval estimation more informative than point estimation?

### 4.3 Hypothesis Testing: Concepts and Procedures

#### 4.3.1 Definition and purpose of hypothesis testing

**Hypothesis testing** is a statistical procedure used to evaluate assumptions or claims about a population based on sample data. It helps researchers and managers make decisions under uncertainty by determining whether observed results are due to chance or reflect real differences. In business, hypothesis testing is used to test claims such as “a new marketing strategy increases sales” or “customer satisfaction has improved.”

Fill in the blank: Hypothesis testing is a statistical procedure used to evaluate \_\_\_\_\_ about a population.

#### 4.3.2 Null and alternative hypotheses

The **null hypothesis ( $H_0$ )** states that there is no effect or difference, while the **alternative hypothesis ( $H_1$ )** states that there is an effect or difference. For example,  $H_0$ : “The new training program has no impact on productivity,” versus  $H_1$ : “The new training program increases productivity.”

Fill in the blank: The null hypothesis states that there is \_\_\_\_\_ effect or difference.



**TABLE 4.3 EXAMPLES OF NULL AND ALTERNATIVE HYPOTHESES**

| Null Hypothesis ( $H_0$ )                            | Alternative Hypothesis ( $H_1$ )                 |
|------------------------------------------------------|--------------------------------------------------|
| Average customer spending is \$50                    | Average customer spending is not \$50            |
| The new marketing campaign has no effect             | The new marketing campaign increases sales       |
| Less than 10% of products are defective              | More than 10% of products are defective          |
| Customer satisfaction scores have not improved       | Customer satisfaction scores have improved       |
| The new drug is not more effective than the old drug | The new drug is more effective than the old drug |

Table 4.3 Examples of Null and Alternative Hypotheses

### 4.3.3 Type I and Type II errors

- **Type I error:** Rejecting a true null hypothesis (false positive).
- **Type II error:** Failing to reject a false null hypothesis (false negative). In business, a Type I error might mean wrongly concluding that a new product is effective, while a Type II error might mean failing to recognise a truly effective product.

Fill in the blank: A Type I error occurs when a true null hypothesis is \_\_\_\_\_.

### 4.3.4 Levels of significance and p-values



The **level of significance ( $\alpha$ )** is the probability of rejecting the null hypothesis when it is true, commonly set at 0.05 (5%). The **p-value** indicates the probability of obtaining the observed results if the null hypothesis is true. If the p-value is less than  $\alpha$ , the null hypothesis is rejected.

Fill in the blank: If the p-value is less than the level of significance, the \_\_\_\_\_ hypothesis is rejected.

#### Pilot questions 4.3

1. What is the purpose of hypothesis testing?
2. Fill in the blank: The null hypothesis states that there is \_\_\_\_\_ effect or difference.
3. What is the difference between Type I and Type II errors?
4. What does the level of significance represent?
5. When is the null hypothesis rejected based on the p-value?

### 4.4 Hypothesis Testing: Applications

#### 4.4.1 Testing means and proportions

Hypothesis testing can be applied to determine whether the mean or proportion of a sample differs significantly from a population value or another sample.

- **Testing means:** For example, testing whether the average monthly sales after a new marketing campaign are higher than before.
- **Testing proportions:** For example, testing whether the proportion of satisfied customers has increased after introducing a new service.

Fill in the blank: Testing means involves comparing the sample mean to the \_\_\_\_\_ mean or another sample mean.

#### 4.4.2 Chi-square tests

The **chi-square test** is used to test relationships between categorical variables. It compares observed frequencies with expected frequencies to determine whether differences are due to chance. In business, chi-square tests can be used to analyse customer preferences across product categories or evaluate the effectiveness of marketing campaigns.

Fill in the blank: The chi-square test compares observed frequencies with \_\_\_\_\_ frequencies.

#### 4.4.3 Business applications of hypothesis testing

Hypothesis testing is widely applied in business decision-making. Examples include:

- Testing whether a new product increases sales.
- Evaluating if customer satisfaction scores differ across regions.



- Determining whether employee training improves productivity. These applications help managers make evidence-based decisions and reduce reliance on guesswork.

Fill in the blank: Hypothesis testing helps managers make \_\_\_\_\_ decisions rather than relying on guesswork.

#### Pilot questions 4.4

1. What is the purpose of testing means in hypothesis testing?
2. Fill in the blank: The chi-square test compares observed frequencies with \_\_\_\_\_ frequencies.
3. Give one example of how hypothesis testing can be applied to customer satisfaction.
4. Why is hypothesis testing important in business decision-making?
5. What type of data is most suitable for chi-square tests?

### Series Summary

This Series introduced you to three key pillars of statistical inference: **sampling theory**, **estimation**, and **hypothesis testing**. You learned why sampling is necessary, the different methods of selecting samples, and the risks of errors and biases. We then explored estimation, distinguishing between point and interval estimation, and interpreting confidence intervals. Finally, we studied hypothesis testing, beginning with its concepts and procedures (null and alternative hypotheses, Type I and II errors, significance levels, and p-values), and concluding with practical applications such as testing means, proportions, and using chi-square tests.

By completing this Series, you should now be able to design representative samples, estimate population parameters, and apply hypothesis testing to support evidence-based business decisions.

### Glossary of Terms

- **Sampling:** Selecting a subset of individuals/items from a population to represent the whole.
- **Random sampling:** Every member of the population has an equal chance of selection.
- **Stratified sampling:** Dividing the population into groups (strata) and sampling from each.
- **Systematic sampling:** Selecting every nth item from a list.
- **Cluster sampling:** Dividing the population into clusters and sampling entire clusters.
- **Sampling error:** Random variation causing the sample to differ from the population.
- **Bias:** Systematic favouring of certain outcomes in sampling.
- **Point estimation:** A single value used to approximate a population parameter.



- **Interval estimation:** A range of values within which a population parameter is likely to fall.
- **Confidence interval:** Interval estimate with a specified probability of containing the true parameter.
- **Hypothesis testing:** A procedure for evaluating claims about a population using sample data.
- **Null hypothesis ( $H_0$ ):** Assumes no effect or difference.
- **Alternative hypothesis ( $H_1$ ):** Assumes an effect or difference exists.
- **Type I error:** Rejecting a true null hypothesis.
- **Type II error:** Failing to reject a false null hypothesis.
- **Level of significance ( $\alpha$ ):** Probability of rejecting  $H_0$  when it is true.
- **p-value:** Probability of obtaining observed results if  $H_0$  is true.
- **Chi-square test:** Test comparing observed and expected frequencies for categorical data.

### Concept Check Questions [Series 4]

#### Objective questions

1. Sampling is the process of selecting a \_\_\_\_\_ from a population. (SLO 4.1)
2. In \_\_\_\_\_ sampling, every member of the population has an equal chance of being selected. (SLO 4.2)
3. A point estimate is a \_\_\_\_\_ value used to approximate a population parameter. (SLO 4.4)
4. The null hypothesis states that there is \_\_\_\_\_ effect or difference. (SLO 4.8)
5. The chi-square test compares observed frequencies with \_\_\_\_\_ frequencies. (SLO 4.12)

#### Short-answer questions

6. Define stratified sampling and give one business example. (SLO 4.2)
7. What are the properties of a good estimator? (SLO 4.4)
8. Explain the difference between Type I and Type II errors. (SLO 4.9)
9. What does the p-value represent in hypothesis testing? (SLO 4.10)
10. Give one example of how hypothesis testing can be applied to customer satisfaction. (SLO 4.13)

#### Long-answer questions



11. Analyse the strengths and limitations of different sampling methods in business research. (SLO 4.2, 4.3)
12. Evaluate the importance of hypothesis testing in business decision-making, with examples. (SLO 4.13)

### Answers to Concept Check Questions [Series 4]

#### Objective questions

1. Subset.
2. Random.
3. Single.
4. No.
5. Expected.

#### Short-answer questions

6. Stratified sampling divides the population into groups and samples from each. *Example:* Sampling customers by income level to study spending habits.
7. Good estimators are unbiased, consistent, and efficient.
8. Type I error: Rejecting a true null hypothesis. Type II error: Failing to reject a false null hypothesis.
9. The p-value represents the probability of obtaining observed results if the null hypothesis is true.
10. Testing whether customer satisfaction scores improved after introducing a loyalty program.

#### Long-answer questions

11. *Strengths:* Random sampling avoids bias; stratified ensures representation; systematic is simple; cluster reduces cost. *Limitations:* Random may be impractical; stratified requires detailed knowledge; systematic risks periodic bias; cluster may reduce accuracy.
12. Hypothesis testing provides a structured way to evaluate claims. *Examples:* Testing if a new product increases sales, if training improves productivity, or if satisfaction differs across regions. It reduces guesswork and supports evidence-based decisions.

## Answers to Pilot Questions

### Part 4.1 Sampling Theory

1. Sampling is the process of selecting a subset of individuals or items from a population.
2. **Random sampling.**



3. Example: Dividing customers into income groups and selecting samples from each group (stratified sampling).
4. Sampling error occurs due to random variation; bias occurs due to systematic favouring of certain outcomes.
5. Minimising bias ensures research results are reliable and decisions are not misleading.

## Part 4.2 Estimation

1. Point estimation is using sample data to calculate a single value that approximates a population parameter.
2. **Population** parameter.
3. Properties of a good estimator: unbiased, consistent, and efficient.
4. Example: A confidence interval can estimate the average amount customers spend per month.
5. Interval estimation is more informative because it provides a range and accounts for uncertainty.

## Part 4.3 Hypothesis Testing: Concepts and Procedures

1. The purpose of hypothesis testing is to evaluate claims about a population using sample data.
2. **No** effect or difference.
3. Type I error: Rejecting a true null hypothesis. Type II error: Failing to reject a false null hypothesis.
4. The level of significance represents the probability of rejecting the null hypothesis when it is true.
5. The null hypothesis is rejected when the p-value is less than the level of significance ( $\alpha$ ).

## Part 4.4 Hypothesis Testing: Applications

1. Testing means helps determine whether the sample mean differs significantly from the population mean or another sample mean.
2. **Expected** frequencies.
3. Example: Testing whether customer satisfaction scores improved after introducing a loyalty program.
4. Hypothesis testing is important because it supports evidence-based business decisions rather than guesswork.
5. Chi-square tests are most suitable for **categorical data**.



# Series 5: Regression, Correlation, Index Numbers, and Time Series Analysis

## Outline of Parts

- **Part 5.1 Correlation Analysis**
  - 5.1.1 Definition and importance of correlation
  - 5.1.2 Types of correlation (positive, negative, zero)
  - 5.1.3 Methods of measuring correlation (Pearson's coefficient, Spearman's rank)
  - 5.1.4 Business applications of correlation
- **Part 5.2 Regression Analysis**
  - 5.2.1 Definition and purpose of regression
  - 5.2.2 Simple linear regression (equation, interpretation, applications)
  - 5.2.3 Multiple regression basics
  - 5.2.4 Business applications of regression
- **Part 5.3 Index Numbers**
  - 5.3.1 Definition and uses of index numbers
  - 5.3.2 Types of index numbers (price, quantity, value)
  - 5.3.3 Methods of constructing index numbers (Laspeyres, Paasche, Fisher's Ideal)
  - 5.3.4 Applications of index numbers in business and economics
- **Part 5.4 Time Series Analysis**
  - 5.4.1 Definition and components of time series (trend, seasonal, cyclical, irregular)
  - 5.4.2 Methods of time series analysis (moving averages, least squares trend fitting)
  - 5.4.3 Forecasting using time series
  - 5.4.4 Business applications of time series analysis

## Introduction

In business statistics, understanding relationships between variables and tracking changes over time is essential for effective decision-making. **Correlation and regression analysis** provide tools to measure and model relationships between variables, helping managers predict outcomes and identify key drivers of performance. **Index numbers** allow comparisons across time or regions by summarising complex data into simple measures, such as price indices or cost-of-living indices. Finally, **time series analysis** equips businesses with techniques to study data collected over time, identify patterns such as trends and seasonality, and make forecasts for planning and strategy.

The aim of this Series is to equip learners with the ability to analyse relationships between variables, construct and interpret index numbers, and apply time series methods for forecasting.



We begin with correlation analysis, exploring definitions, types, and measurement methods. Next, regression analysis introduces simple and multiple regression models and their business applications. We then move to index numbers, covering types, construction methods, and uses. Finally, time series analysis examines components, methods, and forecasting applications.

By the end of this Series, you will be able to measure relationships, build regression models, interpret index numbers, and apply time series techniques to support evidence-based business and economic decisions.

## Series Learning Outcomes

Upon completing **Series 5**, you should be able to:

- **5.1** define correlation and explain its importance in business research,
- **5.2** distinguish between types of correlation (positive, negative, zero),
- **5.3** compute and interpret correlation coefficients (Pearson's and Spearman's),
- **5.4** apply correlation analysis to business decision-making scenarios,
- **5.5** define regression and explain its purpose in modelling relationships,
- **5.6** construct and interpret simple linear regression equations,
- **5.7** explain the basics of multiple regression and its applications,
- **5.8** apply regression analysis to predict business outcomes,
- **5.9** define index numbers and explain their uses in economics and business,
- **5.10** distinguish between types of index numbers (price, quantity, value),
- **5.11** compute index numbers using Laspeyres, Paasche, and Fisher's methods,
- **5.12** apply index numbers to measure inflation, cost of living, and productivity,
- **5.13** define time series and identify its components (trend, seasonal, cyclical, irregular),
- **5.14** apply methods of time series analysis (moving averages, least squares trend fitting),
- **5.15** use time series techniques for forecasting in business contexts.

### 5.1 Correlation Analysis

#### 5.1.1 Definition and importance of correlation

**Correlation** measures the strength and direction of the relationship between two variables. It helps determine whether changes in one variable are associated with changes in another. In business, correlation is important for identifying patterns such as the relationship between advertising expenditure and sales, or employee training and productivity.

Fill in the blank: Correlation measures the strength and \_\_\_\_\_ of the relationship between two variables.



## FIGURE 5.1 TYPES OF CORRELATION ILLUSTRATED WITH SCATTER PLOTS

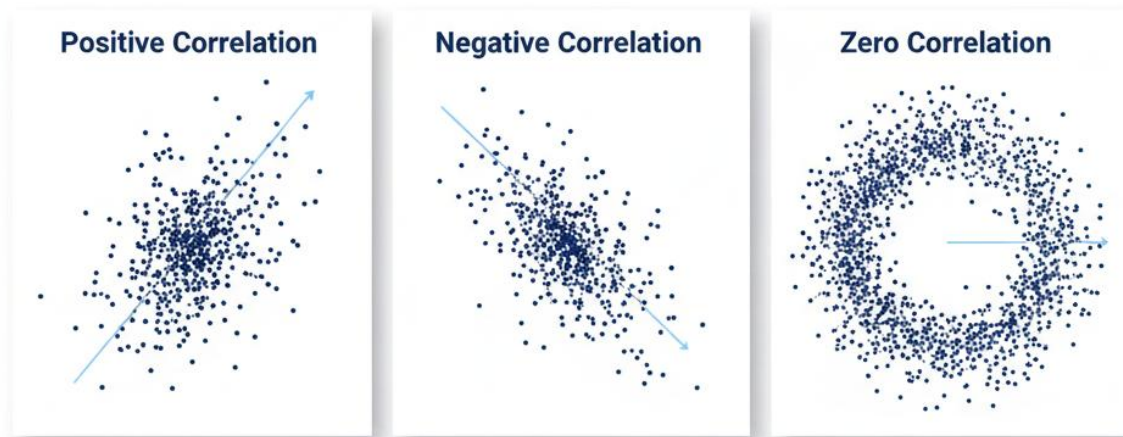


Figure 5.1 Types of Correlation Illustrated with Scatter Plots

### 5.1.2 Types of correlation

- **Positive correlation:** Both variables increase together (e.g., advertising spend and sales revenue).
- **Negative correlation:** One variable increases while the other decreases (e.g., price and demand).
- **Zero correlation:** No relationship between the variables (e.g., shoe size and exam scores).

Fill in the blank: When one variable increases while the other decreases, the correlation is \_\_\_\_\_.



## TABLE 5.1 TYPES OF CORRELATION WITH EXAMPLES

Table 5.1 Types of Correlation with Examples

| Type of Correlation         | Definition                            | Business Application Example           |
|-----------------------------|---------------------------------------|----------------------------------------|
| <b>Positive Correlation</b> | Variables move in the same direction  | Advertising spending and sales revenue |
| <b>Negative Correlation</b> | Variables move in opposite directions | Product price and demand               |
| <b>Zero Correlation</b>     | No consistent relationship            | No employee shoe size and salary       |

### 5.1.3 Methods of measuring correlation

- **Pearson's correlation coefficient (r):** Measures linear relationship between two continuous variables, ranging from  $-1$  to  $+1$ .
- **Spearman's rank correlation:** Measures monotonic relationships using ranked data, useful when data is ordinal or not normally distributed.

Fill in the blank: Pearson's correlation coefficient ranges from \_\_\_\_\_ to  $+1$ .

### 5.1.4 Business applications of correlation

Correlation analysis is widely applied in business to:



- Assess the relationship between marketing spend and sales growth.
- Evaluate the link between employee training and productivity.
- Study the relationship between customer satisfaction and loyalty.
- Analyse financial data such as stock returns and market indices.

Fill in the blank: Correlation analysis helps businesses assess the relationship between marketing spend and \_\_\_\_\_ growth.

#### Pilot questions 5.1

1. What does correlation measure?
2. Fill in the blank: When one variable increases while the other decreases, the correlation is \_\_\_\_\_.
3. What is the range of Pearson's correlation coefficient?
4. Give one example of positive correlation in business.
5. Why is correlation analysis important for managers?

## 5.2 Regression Analysis

### 5.2.1 Definition and purpose of regression

**Regression analysis** is a statistical technique used to model and analyse the relationship between a dependent variable and one or more independent variables. It helps predict outcomes and quantify the strength of relationships. In business, regression is used to forecast sales based on advertising spend, or to analyse how employee training affects productivity.

Fill in the blank: Regression analysis models the relationship between a dependent variable and \_\_\_\_\_ variables.



## FIGURE 5.2 REGRESSION LINE ILLUSTRATING RELATIONSHIP BETWEEN SALES AND ADVERTISING SPEND

Regression Analysis: Sales vs. Advertising Spend

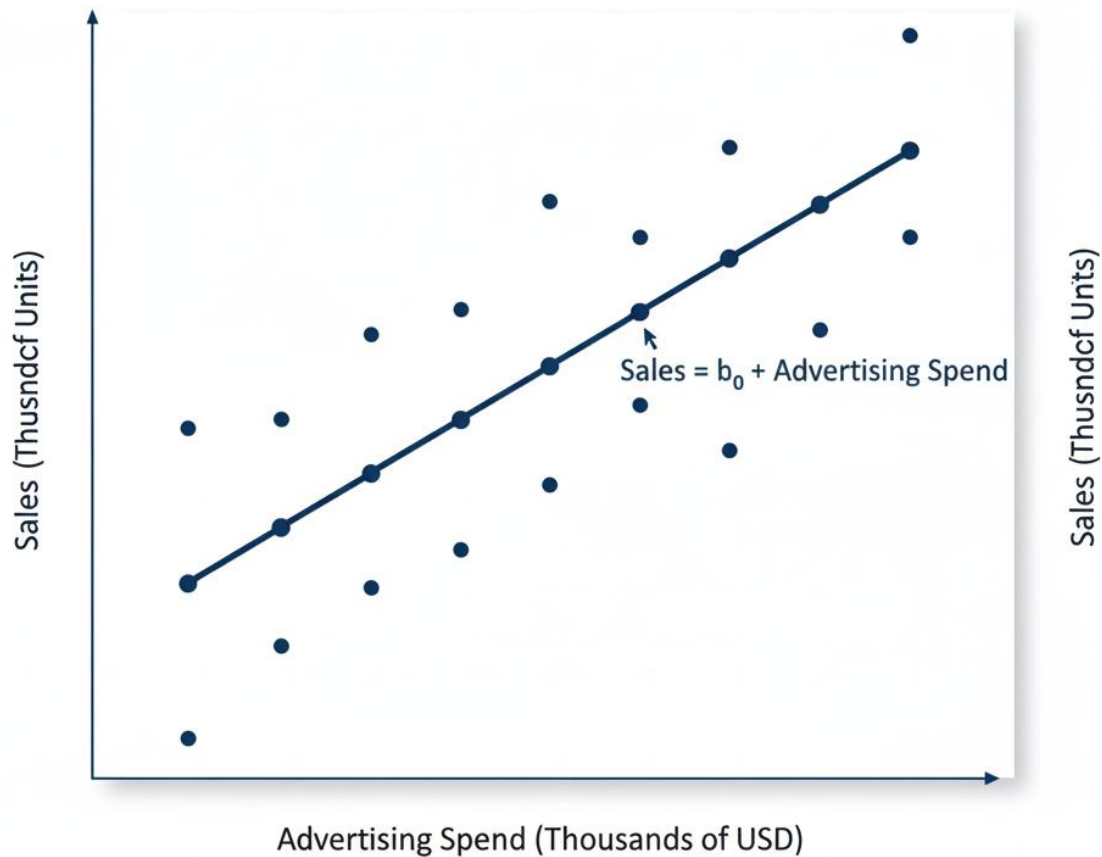


Figure 5.2 Regression Line Illustration Between Sales and Advertising Spend

### 5.2.2 Simple linear regression

Simple linear regression involves one independent variable and one dependent variable.

- **Equation:**  $Y = a + bX$ 
  - $Y$ : dependent variable
  - $X$ : independent variable
  - $a$ : intercept
  - $b$ : slope (rate of change)
- **Interpretation:** The slope indicates how much  $Y$  changes for a one-unit change in  $X$ .



- **Applications:** Predicting sales from advertising spend, estimating productivity from training hours.

Fill in the blank: In simple linear regression, the slope indicates how much the dependent variable changes for a one-unit change in the \_\_\_\_\_ variable.

### 5.2.3 Multiple regression basics

**Multiple regression** extends simple regression to include two or more independent variables.

- **Equation:**  $Y = a + b_1X_1 + b_2X_2 + \dots + b_nX_n$
- **Purpose:** To analyse the combined effect of multiple factors on a dependent variable.
- **Applications:** Predicting sales based on advertising spend, product price, and customer income.

Fill in the blank: Multiple regression includes two or more \_\_\_\_\_ variables to explain variation in the dependent variable.

### 5.2.4 Business applications of regression

Regression analysis is widely applied in business to:

- Forecast sales based on advertising, pricing, and market conditions.
- Analyse the impact of employee training on productivity.
- Predict customer demand based on income and product price.
- Evaluate financial performance using economic indicators.

Fill in the blank: Regression analysis helps businesses forecast \_\_\_\_\_ based on advertising, pricing, and market conditions.

#### Pilot questions 5.2

1. What is regression analysis used for?
2. Fill in the blank: In simple linear regression, the slope indicates how much the dependent variable changes for a one-unit change in the \_\_\_\_\_ variable.
3. Write the general equation for multiple regression.
4. Give one example of regression analysis applied to sales forecasting.
5. Why is regression analysis important in business decision-making?

## 5.3 Index Numbers

### 5.3.1 Definition and uses of index numbers

**Index numbers** are statistical measures designed to show changes in a variable or group of related variables over time, location, or other conditions. They simplify complex data into a single figure that reflects relative change. In business and economics, index numbers are used to measure inflation, cost of living, productivity, and stock market performance.



Fill in the blank: Index numbers are statistical measures designed to show \_\_\_\_\_ in a variable or group of variables.

### 5.3.2 Types of index numbers

- **Price index:** Measures changes in prices of goods and services (e.g., Consumer Price Index).
- **Quantity index:** Measures changes in quantities produced or consumed.
- **Value index:** Measures changes in total value (price  $\times$  quantity).

Fill in the blank: The Consumer Price Index (CPI) is an example of a \_\_\_\_\_ index.

### 5.3.3 Methods of constructing index numbers

- **Laspeyres method:** Uses base-year quantities as weights.
- **Paasche method:** Uses current-year quantities as weights.
- **Fisher's Ideal index:** Geometric mean of Laspeyres and Paasche indices, considered more accurate.

Fill in the blank: The Laspeyres method uses \_\_\_\_\_-year quantities as weights.

### 5.3.4 Applications of index numbers in business and economics

Index numbers are widely applied to:

- Measure inflation and cost of living.
- Track productivity changes in industries.
- Compare economic performance across countries.
- Monitor stock market trends.

Fill in the blank: Index numbers are widely applied to measure \_\_\_\_\_ and cost of living.

#### Pilot questions 5.3

1. What are index numbers used for in business and economics?
2. Fill in the blank: The Consumer Price Index (CPI) is an example of a \_\_\_\_\_ index.
3. What is the difference between Laspeyres and Paasche methods?
4. Give one example of how index numbers can be applied to productivity analysis.
5. Why is Fisher's Ideal index considered more accurate than Laspeyres or Paasche?

### 5.4 Time Series Analysis



### 5.4.1 Definition and components of time series

A **time series** is a sequence of data points collected or recorded at successive points in time, often at equal intervals. Time series analysis helps identify patterns and trends in data over time. The main components of a time series are:

- **Trend:** Long-term upward or downward movement.
- **Seasonal variation:** Regular fluctuations within a year (e.g., holiday sales).
- **Cyclical variation:** Long-term oscillations tied to economic cycles.
- **Irregular variation:** Random or unpredictable fluctuations.

Fill in the blank: A time series is a sequence of data points collected at successive points in \_\_\_\_\_.

### 5.4.2 Methods of time series analysis

- **Moving averages:** Smooth out short-term fluctuations to highlight long-term trends.
- **Least squares trend fitting:** Fits a straight line or curve to data to estimate the trend.
- **Decomposition methods:** Separate time series into trend, seasonal, cyclical, and irregular components.

Fill in the blank: Moving averages are used to smooth out short-term \_\_\_\_\_ in time series data.

### 5.4.3 Forecasting using time series

Forecasting involves predicting future values based on past patterns. Time series forecasting is widely used in business for:

- Sales forecasting
- Demand planning
- Budgeting and financial projections
- Workforce scheduling

Fill in the blank: Time series forecasting involves predicting \_\_\_\_\_ values based on past patterns.

### 5.4.4 Business applications of time series analysis

Time series analysis is applied in business to:

- Identify long-term trends in sales and revenue.
- Detect seasonal demand patterns for inventory management.
- Forecast economic indicators such as GDP or inflation.
- Plan marketing campaigns around cyclical consumer behaviour.



Fill in the blank: Time series analysis helps businesses identify long-term \_\_\_\_\_ in sales and revenue.

#### Pilot questions 5.4

1. What is a time series?
2. Fill in the blank: Moving averages are used to smooth out short-term \_\_\_\_\_ in time series data.
3. Name the four components of a time series.
4. Give one example of time series forecasting in business.
5. Why is time series analysis important for inventory management?

### Series Summary

This Series introduced you to four powerful tools of business statistics: **correlation analysis**, **regression analysis**, **index numbers**, and **time series analysis**. You learned how correlation measures the strength and direction of relationships between variables, and how regression models those relationships to make predictions. We then explored index numbers, which simplify complex data into measures of relative change, and finally time series analysis, which examines data collected over time to identify trends, seasonal patterns, and forecast future values.

By completing this Series, you should now be able to measure relationships between variables, construct regression models, compute and interpret index numbers, and apply time series techniques for forecasting and decision-making in business contexts.

### Glossary of Terms

- **Correlation:** Statistical measure of the strength and direction of a relationship between two variables.
- **Positive correlation:** Both variables increase together.
- **Negative correlation:** One variable increases while the other decreases.
- **Pearson's correlation coefficient (r):** Measures linear correlation between two continuous variables.
- **Spearman's rank correlation:** Measures correlation using ranked data.
- **Regression analysis:** Technique for modelling relationships between dependent and independent variables.
- **Simple linear regression:** Regression with one independent variable.
- **Multiple regression:** Regression with two or more independent variables.
- **Index numbers:** Measures showing relative changes in variables over time or across conditions.



- **Price index:** Measures changes in prices (e.g., CPI).
- **Quantity index:** Measures changes in quantities produced or consumed.
- **Value index:** Measures changes in total value (price  $\times$  quantity).
- **Laspeyres index:** Uses base-year quantities as weights.
- **Paasche index:** Uses current-year quantities as weights.
- **Fisher's Ideal index:** Geometric mean of Laspeyres and Paasche indices.
- **Time series:** Sequence of data points collected over time.
- **Trend:** Long-term movement in time series data.
- **Seasonal variation:** Regular fluctuations within a year.
- **Cyclical variation:** Long-term oscillations tied to economic cycles.
- **Irregular variation:** Random fluctuations in time series data.
- **Moving averages:** Method to smooth short-term fluctuations.
- **Least squares trend fitting:** Method to fit a line or curve to time series data.

### Concept Check Questions [Series 5]

#### Objective questions

1. Correlation measures the strength and \_\_\_\_\_ of the relationship between two variables. (SLO 5.1)
2. Pearson's correlation coefficient ranges from  $-1$  to \_\_\_\_\_. (SLO 5.3)
3. In simple linear regression, the slope indicates how much the dependent variable changes for a one-unit change in the \_\_\_\_\_ variable. (SLO 5.6)
4. The Consumer Price Index (CPI) is an example of a \_\_\_\_\_ index. (SLO 5.10)
5. Moving averages are used to smooth out short-term \_\_\_\_\_ in time series data. (SLO 5.14)

#### Short-answer questions

6. Define negative correlation and give one business example. (SLO 5.2)
7. What is the general equation for simple linear regression? (SLO 5.6)
8. Explain the difference between Laspeyres and Paasche indices. (SLO 5.11)
9. Name the four components of a time series. (SLO 5.13)
10. Give one example of time series forecasting in business. (SLO 5.15)

#### Long-answer questions



11. Analyse the strengths and limitations of correlation and regression analysis in business decision-making. (SLO 5.4, 5.8)

12. Evaluate the importance of index numbers and time series analysis in economic and business forecasting. (SLO 5.12, 5.15)

### Answers to Concept Check Questions [Series 5]

#### Objective questions

1. Direction.
2. +1.
3. Independent.
4. Price.
5. Fluctuations.

#### Short-answer questions

6. Negative correlation occurs when one variable increases while the other decreases.

*Example:* Price and demand.

7.  $Y = a + bX$

8. Laspeyres uses base-year quantities as weights; Paasche uses current-year quantities.

9. Trend, seasonal, cyclical, irregular.

10. Forecasting monthly sales for a retail store.

#### Long-answer questions

11. *Strengths:* Correlation and regression quantify relationships and support predictions.

*Limitations:* Correlation does not imply causation; regression requires assumptions (linearity, independence).

12. Index numbers simplify complex data, making inflation and productivity measurable. Time series analysis identifies patterns and supports forecasting. Together, they provide essential tools for planning and policy.

### Answers to Pilot Questions [Series 5]

#### Part 5.1 Correlation Analysis

1. Correlation measures the strength and direction of relationships between variables.
2. Negative.
3. -1 to +1.
4. Example: Advertising spend and sales revenue.
5. It helps managers identify patterns and make informed decisions.



### Part 5.2 Regression Analysis

1. Regression is used to model and predict relationships between variables.
2. Independent.
3.  $Y = a + b_1X_1 + b_2X_2 + \dots + b_nX_n$
4. Example: Forecasting sales based on advertising spend.
5. It supports evidence-based decision-making.

### Part 5.3 Index Numbers

1. Index numbers measure changes in variables over time or conditions.
2. Price.
3. Laspeyres uses base-year weights; Paasche uses current-year weights.
4. Example: Measuring productivity changes in manufacturing.
5. Fisher's Ideal index balances both methods, reducing bias.

### Part 5.4 Time Series Analysis

1. A time series is a sequence of data points collected over time.
2. Fluctuations.
3. Trend, seasonal, cyclical, irregular.
4. Example: Forecasting quarterly demand for electricity.
5. It helps businesses manage inventory by anticipating seasonal demand.

